



A further verification of FZI* and PSRTI: Newly developed petrophysical rock typing indices



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ABSTRACT

Despite the differences between petrophysical static (PSRTs) and dynamic rock types (PDRTs), previous indices were unable to distinguish between them. FZI-Star (FZI*) and PSRTI are recently developed petrophysical dynamic and static rock typing indices, respectively. Considering the importance of rock typing in reservoir characterization and the need for reliable and user-friendly techniques, in this study we attempt to further verify the performance of FZI* and PSRTI by comparing them with FZI, Winland r35, and MFZI using data belonging to a heterogeneous carbonate reservoir from the Asmari Formation. The experimental data set includes 10 primary drainage mercury injection, 29 water-oil, and 45 gas-oil capillary pressure tests for PSRTs prediction in conjunction with 52 water-oil and 51 gas-oil relative permeability data for PDRTs. Moreover, we investigated the correlation between various indices and several petrophysical attributes. We defined these attributes as the integrals of mercury injection capillary pressure, mercury injection threshold capillary pressure, measured r35, capillary pressure, and relative permeability curves along with residual saturations. The results showed that our indices are able to successfully identify static and dynamic rock units with higher accuracy than other indices. Among the other existing methods, Winland r35 was the only one that showed an acceptable outcome; while, FZI, and MFZI underperformed in identifying the existing rock types. Using the experimental data we also propose the empirical equations that can be used to model capillary pressure and relative permeability characteristics of rocks.

1. Introduction

Petrophysical rock typing has a broad range of applications in drilling (e.g., prediction of high fluid-loss zones), production (e.g., identifying potential production/injection zones for locating perforations, and designing diversion systems in acidizing) (Roque et al., 2017; Oliveira et al., 2016), reservoir studies (net-pay cut-off definition) (Kolodzie, 1980; Saboorian-Jooybari, 2017), and permeability prediction in un-cored intervals (Amaefule et al., 1993; Abbaszadeh et al., 1996; Chen and Yao, 2017; Chen and Zhou, 2017). However, its reservoir engineering-related applications such as representative sample selection for special core analysis (SCAL) tests (Siddiqui et al., 2006; Serag El-Din et al., 2014; Mirzaei-Paiaman and Saboorian-Jooybari, 2016; Mirzaei-Paiaman et al., 2018), and defining saturation functions

for reservoir static/dynamic modeling (Mirzaei-Paiaman et al., 2015, 2018; Askari and Behrouz, 2011) are more significant since the outcomes directly affect the simulation models output and their reliability. For instance, rock typing can efficiently reduce the number of representative samples required for SCAL analysis (Mirzaei-Paiaman and Saboorian-Jooybari, 2016). Furthermore, assigning saturation functions to static and dynamic reservoir models requires establishing a clear relationship between saturation functions and laboratory measured rock properties.

So far, it has been assumed that a given rock type can be represented by a unique primary drainage capillary pressure profile along with a set of relative permeability curves (Saboorian-Jooybari et al., 2010; Izadi and Ghalambor, 2013; Ferreira et al., 2015; Mirzaei-Paiaman et al., 2015). However, we showed recently (Mirzaei-Paiaman et al., 2018)

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Nomenclature and list of symbols*Acronyms or Abbreviations*

DRT	Discrete Rock Type
FZI	Flow Zone Indicator
FZI*	FZI-Star (a modified flow zone indicator)
FZI**	FZI-Double Star (a modified flow zone indicator)
<i>J</i> -function	A normalized capillary pressure function
LC	Lorenz Coefficient
MFZI	Modified Flow Zone Indicator
PDRT	Petrophysical Dynamic Rock Type
PSRT	Petrophysical Static Rock Type
PSRTI	Petrophysical Static Rock Type Indicator
SCAL	Special Core Analysis Laboratory

Symbols

C_1	to C_{13} Constant
$\frac{dp}{dx}$	Pressure change per unit length of a porous medium
F_s	Shape factor

k_e	Effective permeability
k_{eg}	Gas effective permeability
k_{eo}	Oil effective permeability
k_{ew}	Water effective permeability
k_r	Relative permeability
$P_{c,g-o}$	Gas-oil capillary pressure
$P_{c,Hg}$	Mercury injection capillary pressure
$P_{c,w-o}$	Water-oil capillary pressure
r_{mh}	Effective or mean hydraulic unit radius
S_{Hg}	Mercury saturation
S_o	Oil saturation
S_{oi}	Initial oil saturation
S_{or}	Residual oil saturation
S_w	Water saturation
S_{wc}	Connate water saturation
P_c	Capillary pressure
v	Fluid velocity or interstitial velocity
τ	Tortuosity
ϕ	Effective connected porosity
A	Constant
k	Absolute permeability

that rocks with a unique primary drainage capillary pressure profile might have a different set of relative permeability curves and vice-versa depending on complexity of the porous medium regardless of wetting conditions. Thus, each saturation function may need a particular rock typing scheme. This led to defining a new petrophysical static (PSRT) and a dynamic rock type (PDRT) which proved rock types might not necessarily overlap or share petrophysical properties, no matter what their wettability is (Mirzaei-Paiaman et al., 2018).

Each petrophysical rock type should be characterized using a quantitative index with routine core data as an input. This facilitates categorization of rock types and can be considered as a more efficient sample selection for SCAL tests. Such a procedure enables us to assign the corresponding saturation functions to the static and dynamic reservoir models. In this regard, core-based petrophysical rock typing methods were classified into three categories (Mirzaei-Paiaman et al., 2018) as follows:

1. Indices that utilize permeability, porosity, and connate water saturation such as cut-off based methods (Rebelle, 2014), empirical (Kolodzie, 1980; Pittman, 1992; Aguilera, 2002) or theoretical ones (Amaefule et al., 1993; Mirzaei-Paiaman et al., 2015, 2018).
2. Capillary pressure-based methods such as *J*-functions, the empirical P_c grouping technique, parameterization (Thomeer, 1960; Xu and Torres-Verdin, 2013; Lin et al., 2015), and measured r_{35} (Kolodzie, 1980).
3. Spontaneous imbibition rate-driven method of FZI** or “FZI-Double Star” developed by Mirzaei-Paiaman and Saboorian-Jooybari (2016).

Among these, the first category is of special interest since it generally does not require prior knowledge of capillary pressure and/or relative permeability data, but to some extent uses SCAL-driven parameters (Nooruddin and Hossain, 2011; Izadi and Ghalambor, 2013). Despite the differences between PSRT and PDRT, current indices are not able to distinguish between static and dynamic rock types (Mirzaei-Paiaman et al., 2018). Furthermore, since theoretical indices (Amaefule et al., 1993; Nooruddin and Hossain, 2011; Izadi and Ghalambor, 2013) are mainly based on a generalized form of the Kozeny-Carman equation, then the outcome (e.g., FZI by Amaefule et al. (1993)) is a function of grain size rather than pore throat diameter. Depending on the pore network complexity, significant errors can be introduced to rock typing results. Also, empirical indices are not universal and are highly

dependent on porous medium properties.

Considering the importance of rock typing in reservoir characterization and the need for reliable and user-friendly techniques, this study attempts to further verify our newly developed petrophysical rock typing approach (Mirzaei-Paiaman et al., 2018). We presented the consistency of our methodology in delineating static and dynamic rock types and its superiority over existing methods. It is noteworthy that none of the previous rock typing indices (Amaefule et al., 1993; Nooruddin and Hossain, 2011; Izadi and Ghalambor, 2013) had been verified using an exhaustive set of SCAL data. Therefore, we utilized a comprehensive set of SCAL data from a heterogeneous Oligocene-Miocene carbonate reservoir from the Asmari Formation in one of the Iranian SW oil fields to examine their reliability. The experimental data contains 10 primary drainage mercury injection, 29 water-oil and 45 gas-oil capillary pressure tests for PSRTs and 52 water-oil and 51 gas-oil relative permeability experiments for PDRTs. In addition to characterize the static and dynamic rock types, we also empirically investigated the correlation between available indices and various petrophysical attributes of the samples.

A further useful verification could be presented here which may support Mirzaei-Paiaman et al. (2018) as:

1. In Mirzaei-Paiaman et al. (2018), the SCAL data that was used to check the models belonged to a reservoir from Albian-Campanian Bangestan group with a dissimilar depositional environment and diagenetic history to the Oligocene-Miocene Asmari Formation. It is vital to further verify or validate the performance of newly developed models against large sets of high quality and reliable data from various resources especially data from complex reservoir systems. This is the only way to have a closer look at the newly developed models and map their strength (i.e., where they perform better against existing models for certain reservoirs) and possible weakness where they are not superior to the existing models.
2. The size and variety of the data used for performance analysis and verification is not comparable to Mirzaei-Paiaman et al. (2018). Mirzaei-Paiaman et al. (2018) studied only the SCAL data in oil-water systems, whereas in the present work the systems of gas-oil tests were also utilized. Incorporation of diverse types of fluid systems enables us to enhance the knowledge of different rock typing indices along with their pros and cons. Such hard data are very valuable for other researchers, as well.
3. The empirical models that are used to model the capillary pressure

and relative permeability characteristics of rocks are also different from Mirzaei-Paibaman et al. (2018).

2. FZI-Star (FZI*) and PSRTI

Using the base form of Kozeny-Carman equation and Darcy's law for single and multiphase flow, an index was introduced to define PDRTs using routine core data (Mirzaei-Paibaman et al., 2018). The base form of Kozeny-Carman equation links the micro-scale characteristics of a porous medium to its permeability and porosity (Kozeny, 1927; Carman, 1937) which can be written as (Mirzaei-Paibaman et al., 2015, 2018):

$$k = \phi \frac{r_{mh}^2}{F_s \tau} \quad (1)$$

where k is the absolute permeability, ϕ is the effective connected porosity, r_{mh} is the effective or mean hydraulic unit radius (defined as the ratio of a cross-sectional area to a wetted perimeter), τ is the tortuosity (defined as the ratio of an actual fluid-travelled length to the system length) (Shen and Chen, 2007), and F_s is the shape factor to account for non-circular capillary tubes ($F_s = 2$ for a circular tube). $\frac{r_{mh}^2}{F_s \tau}$ is a pack of microstructural attributes of sedimentary rocks that control the fluid flow which can vary between $\frac{v}{dp/dx}$ values of different rock types (v is the fluid velocity or interstitial velocity and $\frac{dp}{dx}$ is the pressure change per unit length of a porous medium). When permeability and porosity

are in millidarcy (mD) and fraction, respectively; then FZI* can be expressed in microns to define PDRTs as (Mirzaei-Paibaman et al., 2018):

$$FZI^* = 0.0314 \sqrt{\frac{k}{\phi}} = \frac{r_{mh}}{\sqrt{F_s \tau}} \quad (2)$$

Samples with similar FZI* values should exhibit comparable fluid flow behavior and thus can be bundled as an individual PDRT. For a given PDRT, cross-plot of $0.0314 \sqrt{k}$ vs. $\sqrt{\phi}$ on a log-log scale yields a unite-slope line, and the intercept with $\phi = 1$ will be the FZI*. In opposite, rocks with different FZI* should appear as a series of parallel lines. Finally, permeability in un-cored intervals can be estimated by:

$$k = 1014 \phi (FZI^*)^2 \quad (3)$$

FZI* can also be directly concluded from Darcy's law for 1-D single-phase fluid flow in a homogeneous porous medium when the Darcy velocity is replaced by interstitial velocity (Mirzaei-Paibaman et al., 2018). In a multiphase flow system, if the fluid properties are kept constant then $\frac{k_e}{\phi}$ or $\frac{kk_r}{\phi}$ or $FZI^* k_r$ is the parameter that controls the flow implying that samples with similar flow behavior should present similar $\frac{kk_r}{\phi}$ data (k_e and k_r are the effective and relative permeabilities, respectively). However, this contradicts the common practice in petrophysical rock typing that rocks within one PDRT should have similar relative permeability, k_r , data. Ultimately, k_r is a saturation-dependent property and thus FZI* can be assumed as the index that identifies dynamic rock groups in the multiphase flow system when routine core data is available only.

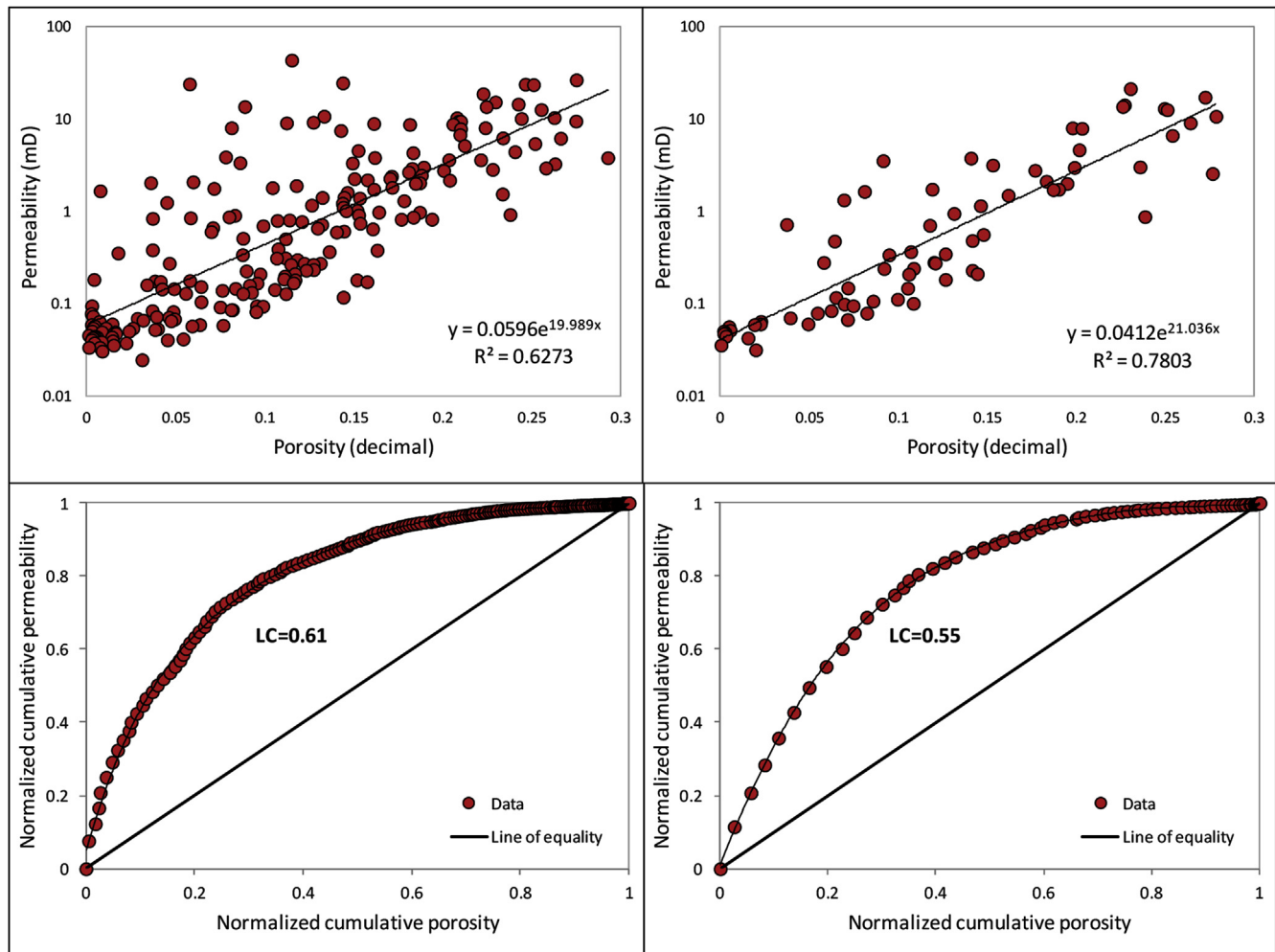


Fig. 1. Porosity-permeability cross-plot and Lorenz plot for horizontal (left) and vertical (right) plugs. The data presented indicates highly heterogeneous nature of the carbonate reservoir rock.

Furthermore, a new index for PSRTs was developed through combining the Young–Laplace capillary pressure expression and the base form of Kozeny–Carman equation (Mirzaei-Paiaman et al., 2018) known as PSRTI:

$$\text{PSRTI} = 0.0314 \sqrt{\frac{k}{\phi}} F_{\text{K}} \tau = \text{FZI}^* \sqrt{F_{\text{K}} \tau} \quad (4)$$

When rock–fluid interaction and fluid properties remain unchanged, cores with similar PSRTI values will exhibit similar primary drainage capillary pressure curves and thus form an individual PSRT. In practice, where $F_{\text{K}} \tau$ is not easy to measure for each rock separately, FZI^* becomes the sole parameter to delineate PSRTs depending on pore geometry complexity among the population of rocks.

3. Data collection

Petrophysical data is collected on core plugs retrieved from a carbonate reservoir in the Asmari Formation located north of the Persian Gulf, SW Iran. Fig. 1 shows the cross-plots of porosity–permeability and the Lorenz plots for horizontal and vertical plugs. In the porosity–permeability cross-plots the correlation coefficients were 0.63 and 0.78 for horizontal and vertical plugs, respectively. Furthermore, the Lorenz Coefficients (LC) were 0.61 (for horizontal plugs) and 0.55 (for vertical plugs). The values of these two indices confirm the heterogeneous nature of the reservoir, especially in the horizontal direction.

4. Results and discussion

4.1. PSRTs

4.1.1. Primary drainage mercury injection capillary pressure data

In this section, we compare the results from FZI^* , FZI, and Winland r35 techniques in defining PSRTs in our samples. FZI (Amaefule et al., 1993) and Winland r35 (Kolodzie, 1980) are expressed in micron, where permeability and porosity are in mD and fraction, respectively, as follows:

$$\text{FZI} = \frac{0.0314 \sqrt{\frac{k}{\phi}}}{\frac{\phi}{1-\phi}} \quad (5)$$

$$\text{Log}(r_{35}) = -0.996 + 0.588 \text{Log}(k) - 0.864 \text{Log}(\phi) \quad (6)$$

The DRT, Discrete Rock Type, equation was used to separate different clusters (Abbaszadeh et. 1996; Mirzaei-Paiaman et al., 2018).

$$\text{DRT no.} = \text{ROUND}(\text{LOG}(\text{index}) + A; 0) \quad (7)$$

In this equation, A is an adjustable constant and is chosen in such a way that the output starts from 1 corresponding to the PSRT no. 1 (i.e., PSRT1). A is 2.6 for FZI^* and 1.6 for both FZI and Winland r35.

The PSRTs that are identified by different methods are shown in Fig. 2 where the data before the threshold pressure point is eliminated based on Mirzaei-Paiaman et al. (2018)'s method. In this figure, the DRT numbers 1, 2, and 3 are represented by red, orange, and green, respectively. It can be found from the following figure that although capillary pressure curves are not following similar trends, FZI identifies only one PSRT; while, FZI^* and Winland r35 recognize two distinct groups of rock types (PSRT1 above PSRT2).

Fig. 3 shows incremental mercury saturation vs. a pore throat radius predicted by three different methods. In this process, we did not include capillary pressure values less than the threshold pressure. A pore throat radius is calculated via the Young–Laplace capillary pressure equation where each PSRT must contain a group of rocks with similar pore throat size distributions. Results confirm that FZI^* performed better than FZI and Winland r35 to separate any existing PSRTs. FZI^* found more distinct pore throat clusters than Winland r35 on two separate PSRTs; while, FZI recognized only one PSRT.

The relationship between different indices and the threshold pressure was investigated (see Supplementary Material). It can be found as the threshold pressure increases, both FZI^* and Winland r35 decrease with correlation coefficients of 0.66 and 0.61, respectively. We were not able to establish a clear relationship between the threshold pressure and FZI, as the correlation is quite poor mainly because this index is a function of grain size rather than pore throat diameter as previously shown by Mirzaei-Paiaman et al. (2018).

In the next step, we plotted different indices vs. measured r35 which is depicted in Supplementary Material. The correlation coefficient between the empirical Winland r35 and the measured r35 was 0.84 and did not approach unity. This emphasizes the non-universality of this equation; while, the correlation coefficient between FZI^* and the measured r35 was 0.84, and FZI and the measured r35 did not exhibit any correlation.

The correlation between these three indices and the area under the capillary pressure curve can be found in Supplementary Material. This area reflects the amount of work that one fluid should do to displace the

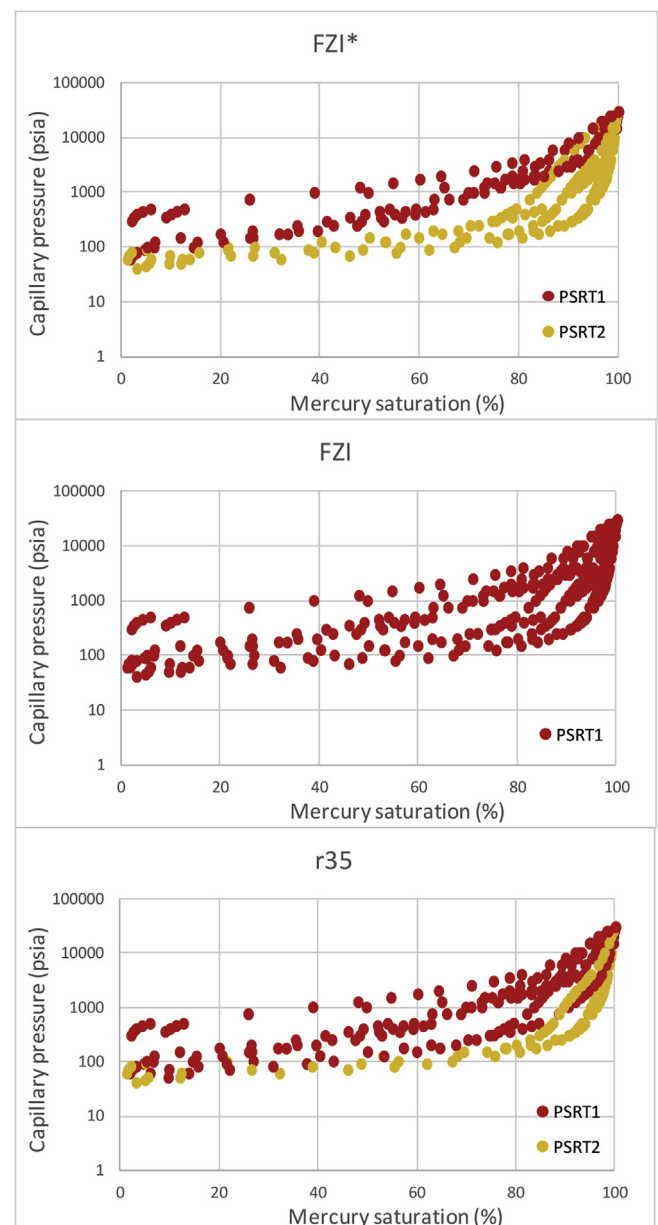


Fig. 2. Identification of PSRTs using mercury injection capillary pressure data by FZI^* (top), FZI (middle), and Winland r35 (bottom).

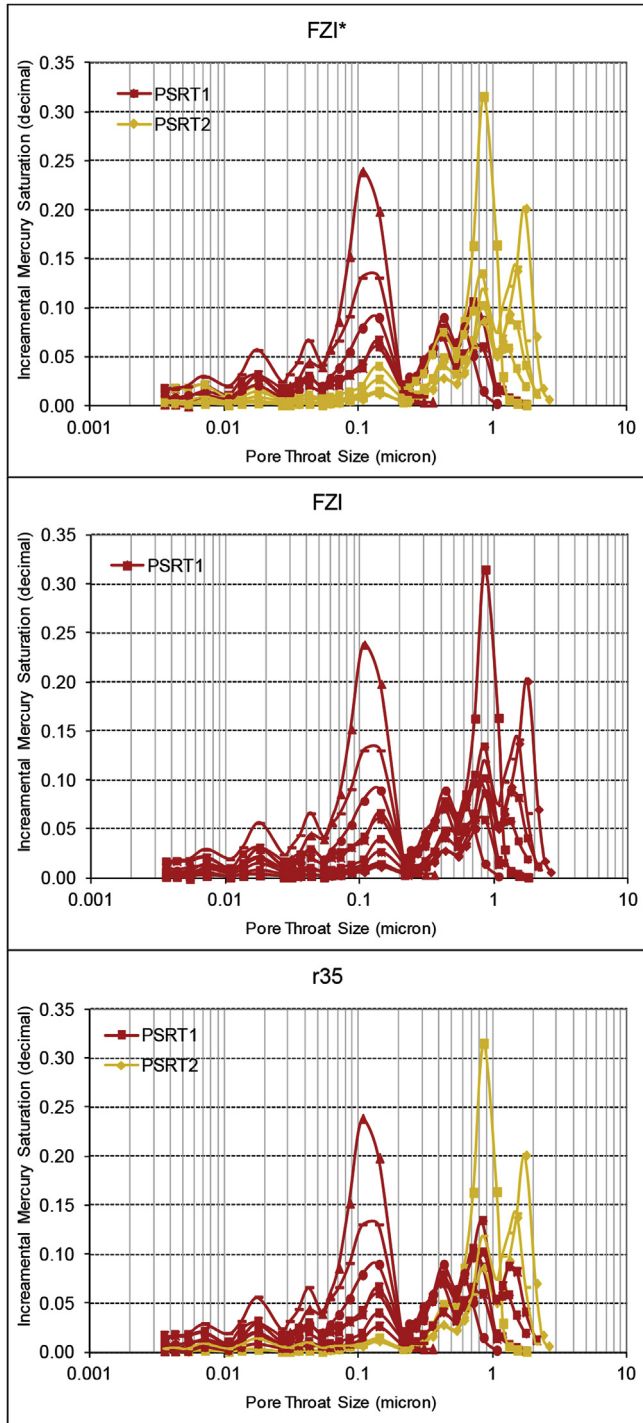


Fig. 3. The incremental mercury saturation vs. pore throat radius and the PSRTs by FZI* (top), FZI (middle) and Winland r35 (bottom).

second fluid through a porous medium (Anderson, 1987). This value is proportional to the pore structure directly. Both FZI* and Winland r35 decrease as the area under the curve increases. This implies that a greater work is needed for fluid displacement. The correlation coefficient was found to be 0.67 and 0.59 for FZI* and Winland r35, respectively. FZI exhibited an opposite trend with a very low correlation coefficient of 0.16; where, an increase in the area under the capillary pressure curve resulted in higher FZI values.

We investigated the relationship between different attributes of mercury injection capillary pressure data and the indices. This leads to a more precise performance characterization of different indices in rock

Table 1
Details of best fitted models to the data.

Experiment	Best fitted model type	Best fitted model	Comments
Primary drainage mercury injection capillary pressure data	Exponential	$P_{c,fig} = C_1 e^{C_2 S_{fig}}$	$P_{c,fig}$ is the measured mercury injection capillary pressure in psia, S_{fig} is the mercury saturation in the core in fraction and varies from 0 to 1, and C_1 and C_2 are constants
Primary drainage water-oil capillary pressure data	Logarithmic	$P_{c,w-o} = -C_3 \ln \left(\frac{S_w - S_{wc}}{1 - S_{wc}} \right)$	$P_{c,w-o}$ is the water-oil capillary pressure in psia, C_3 is a constant, S_{wc} is the connate water saturation in fraction, and S_w is the water saturation in fraction
Primary drainage gas-oil capillary pressure data	Logarithmic	$P_{c,g-o} = -C_4 \ln \left(\frac{S_o - S_{or}}{S_{oi} - S_{or}} \right)$	$P_{c,g-o}$ is the gas-oil capillary pressure in psia, C_4 is a constant, and S_{oi} and S_{or} are the oil saturation, the initial oil saturation and the residual oil saturation, respectively in fraction
Non-zero connate water saturation	Exponential	$P_{c,g-o} = C_5 e^{-C_6 \left(\frac{S_o - S_{or}}{1 - S_{or}} \right)}$	C_5 and C_6 are constants
Zero connate water saturation	Exponential	$P_{c,g-o} = C_7 e^{\frac{C_8 (S_o - S_{or})}{1 - S_{or} - S_{wc}}}$	k_{ew} is the water effective permeability in mD and C_7 and C_8 are constants
Water relative permeability data	Exponential	$\frac{k_{ew}}{\phi} = C_9 e^{\frac{C_{10} (S_w - S_{wc})}{1 - S_{or} - S_{wc}}}$	k_{eo} is the oil effective permeability in mD and C_9 is a constant
Oil relative permeability data	Logarithmic	$\frac{k_{eo}}{\phi} = -C_3 \ln \left(\frac{S_w - S_{wc}}{1 - S_{or} - S_{wc}} \right)$	C_{10} and C_{11} are constants
Oil relative permeability data	Exponential	$\frac{k_{eo}}{\phi} = C_{10} e^{\frac{C_{11} (S_o - S_{or})}{1 - S_{or}}}$	k_{eg} is the gas effective permeability in mD and C_{12} and C_{13} are constants
Gas relative permeability data	Exponential	$\frac{k_{eg}}{\phi} = C_{12} e^{-C_{13} \frac{S_o - S_{or}}{1 - S_{or}}}$	

typing. Later, a quantitative analysis is carried out continuously when dealing with other saturation functions. In the current study, we were also able to demonstrate that saturation functions cannot always be modeled using a specific form of a mathematical function. For example, while an exponential model may give best fit to the relative permeability data of a given formation, it may show poor performance for another formation.

After trying different models, it was found that the mercury injection capillary pressure data could be well represented by an exponential equation (see Table 1).

The quantitative relationship between three separate indices with C_1 and C_2 are shown in Supplementary Material. These constants control the capillary pressure curves. FZI* and Winland r35 showed a decreasing trend as C_1 increases implying a higher capillary pressure that is expected in tighter media. The correlation coefficient of 0.05 confirms there is not a clear relationship between such attributes and FZI. Both FZI* and Winland r35 increased as C_2 increased with acceptable correlation coefficients. Likewise there was not any clear relationship

between C_2 and FZI which means this index is suffering from lack of considering capillary pressure effects.

4.1.2. Primary drainage water-oil capillary pressure data

In addition to FZI*, FZI, and Winland r35, we examined the accuracy of MFZI (Izadi and Ghalambor, 2013). This specific index needs a connate water saturation value, S_{wc} , as an input parameter. To obtain MFZI, $A = 1.6$ was assigned to our data for DRT calculations:

$$MFZI = \frac{0.0314 \sqrt{\frac{k}{\phi}} \times \sqrt{1 - S_{wc}}}{\frac{\phi}{1 - \phi} (1 - S_{wc})^2} \quad (8)$$

Fig. 4 presents the PSRTs that are categorized by each method. FZI*, FZI, and Winland r35, each recognized two PSRTs whereas MFZI recognized three PSRTs. Among all, the indices that produced meaningful groups are FZI* and Winland r35. The PSRT1 that is predicted by FZI* is located reasonably to the right of PSRT2 meaning that at a given water

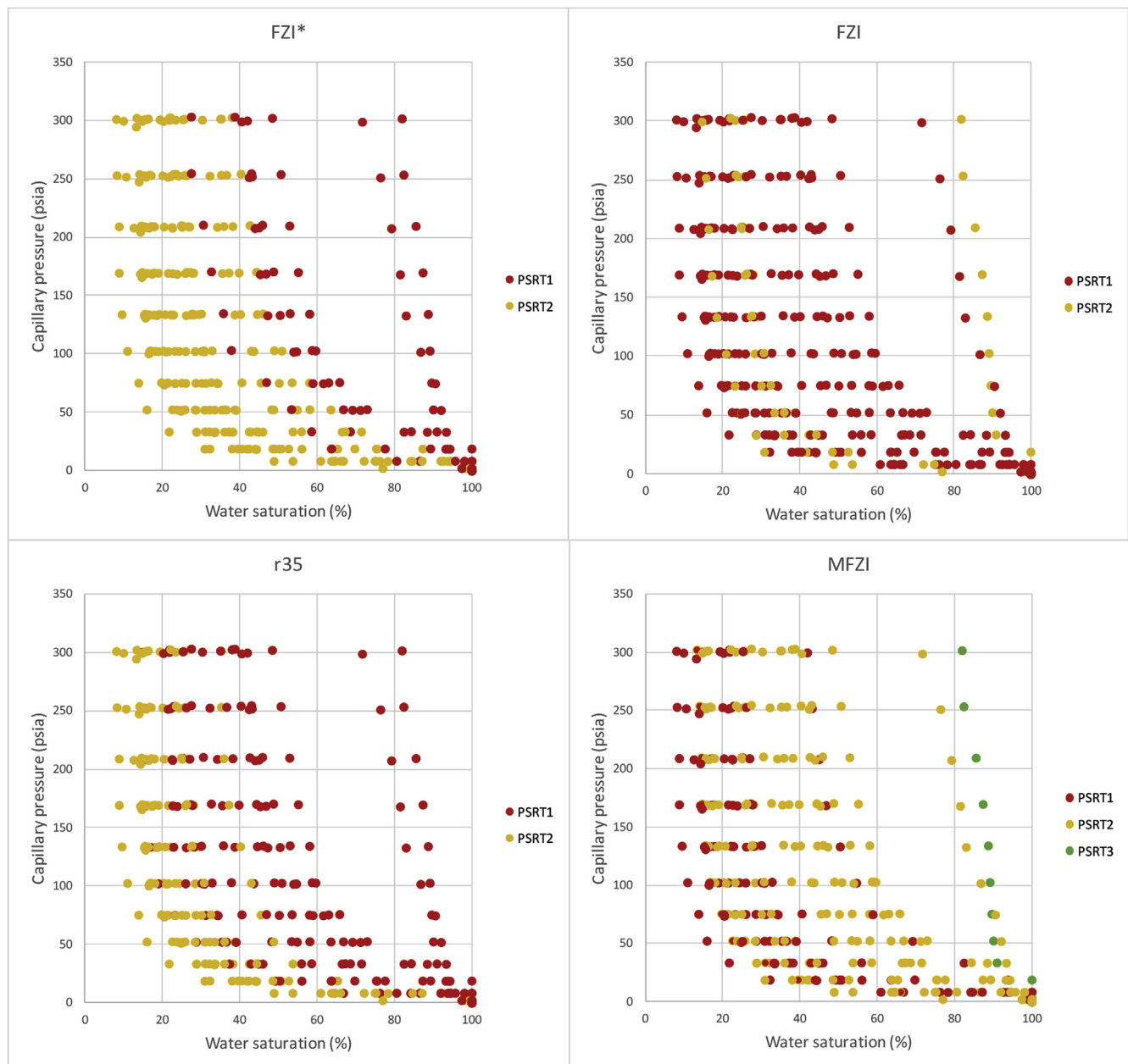


Fig. 4. Identification of PSRTs using water-oil capillary pressure data by FZI* (top left), FZI (top right), MFZI (bottom right), and Winland r35 (bottom left).

saturation, the tight rocks within PSRT1 need a higher displacement pressure. These tight samples are associated with higher connate water saturations, as well. In terms of recognizing distinct clusters, Winland r35 provided us with acceptable predictions, too, however, FZI* is superior. Additionally, FZI and MFZI were unsuccessful in categorizing PSRTs and the identified PSRTs by these two methods did not show separate distinct clusters.

As discussed earlier, tighter rocks should exhibit higher connate water saturations regardless of wettability (Mirzaei-Paibaman et al., 2013). This means as connate water saturation increases if the right rock typing index is chosen, the index should decrease. Hence, we decided to plot different indices vs. connate water saturation, in particular as shown in Supplementary Material for further verifications. Both FZI* and Winland r35 followed the expected trend with R^2 of 0.58 and 0.48, respectively. However, FZI did not demonstrate any meaningful correlation with connate water saturation ($R^2 = 0.03$), and MFZI displayed an opposite trend compared to all, with R^2 of 0.57. It should be noted that the MFZI contains the term S_{wc} .

The quantitative relationship between characteristics of a water-oil capillary pressure curve and different indices was studied, as well. Based on Table 1, logarithmic function represented the data. The relationship between C_3 and various indices is shown in Supplementary Material. In this regard, FZI* and Winland r35 decreased as C_3 increased and a closer look at the mathematical equation that was used confirmed the results. In this case, FZI* generated a higher R^2 of 0.53 compared to 0.47 for Winland r35. There is not any meaningful relationship between C_3 and FZI (i.e., R^2 of 0.04). Also, MFZI demonstrated a trend opposite to FZI* and Winland r35, with R^2 of 0.20.

4.1.3. Primary drainage gas-oil capillary pressure data

4.1.3.1. Gas-oil capillary pressure data (non-zero connate water saturation). The ability of different indices in revealing various PSRTs is demonstrated in Fig. 5 where all indices predicted the existence of

two separate data clusters with clear distinction. In this figure, the liquid saturation is the sum of the oil and connate water saturations.

Four different indices are plotted vs. residual liquid saturation which is obtained after the primary drainage process (see Supplementary Material). Tight rocks are in general associated with higher residual liquid saturations, which is due to their smaller pore throat sizes (Hamidpour et al., 2015; Mirzaei-Paibaman et al., 2010; Harimi et al., 2018). All indices decreased as residual liquid saturation increased. This is in accordance with the expected trend between tightness of porous medium pore throat and residual liquid saturation. FZI* and Winland r35 showed a very strong correlation with residual liquid saturation with R^2 of 0.97 for both, followed by FZI with R^2 of 0.93 and MFZI with R^2 of 0.73.

The quantitative relationship between parameters of a gas-oil capillary pressure curve and different indices was also analyzed and it was found that a logarithmic function can represent the data (see Table 1). The relationship between C_4 and various indices is found in Supplementary Material. It is evident that all indices decrease as C_4 increases and this is in line with mathematical form of the fitted function. FZI* and Winland r35 had the highest correlation coefficients of 0.52 and 0.51, respectively; whereas, FZI and MFZI yielded R^2 of 0.29 and 0.11, correspondingly.

4.1.3.2. Gas-oil capillary pressure data (zero connate water saturation). Fig. 6 explains the PSRTs that are characterized from different indices. Although all indices identified two groups of rocks, FZI* and Winland r35 generated the best results. These two PSRTs that are recognized are mostly separate from one another with some overlaps. FZI and MFZI were incapable of classifying two distinct PSRTs with a clear boundary.

We further analyzed the relationship between the indices and residual oil saturation which is depicted in Supplementary Material. Based on the earlier discussions in this text, a tight porous medium is

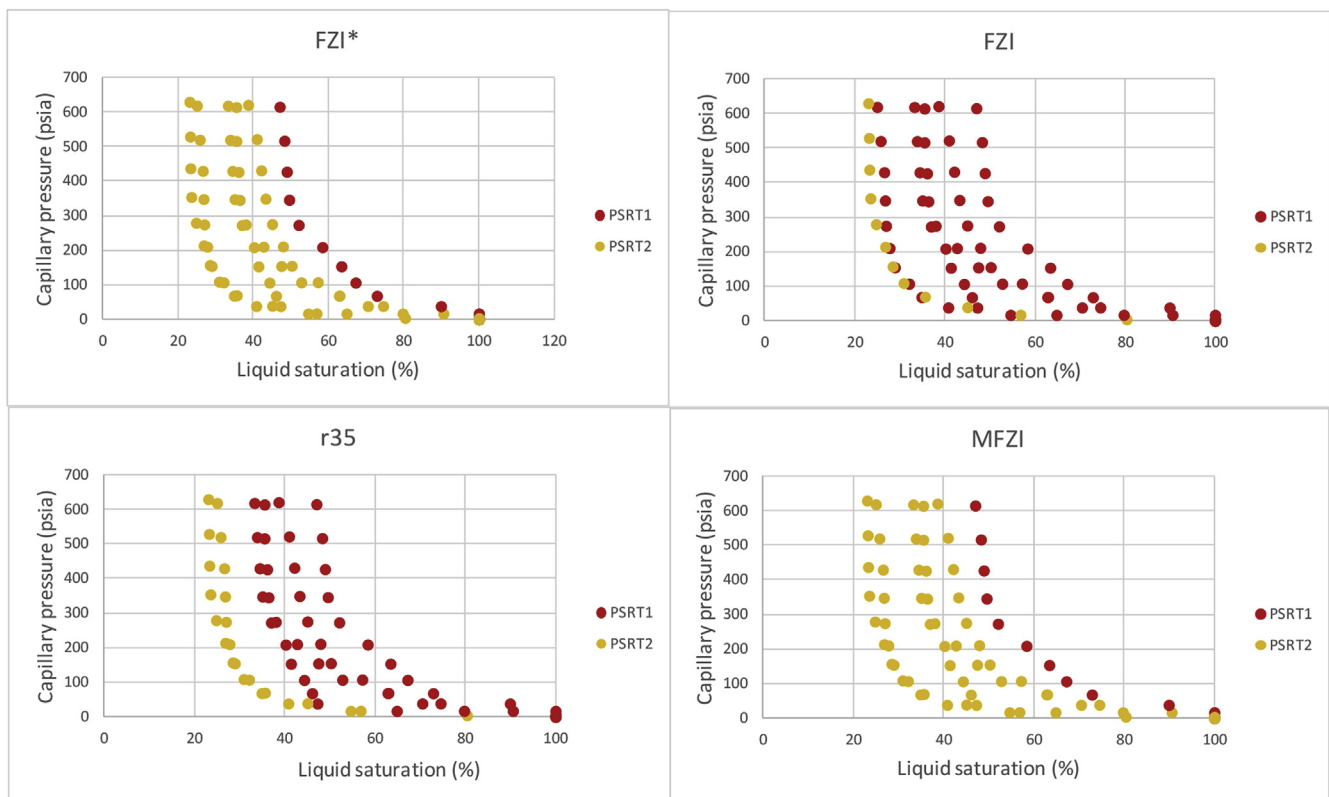


Fig. 5. Identification of PSRTs using gas-oil capillary pressure data (with connate water saturation) by FZI* (top left), FZI (top right), MFZI (bottom right) and Winland r35 (bottom left).

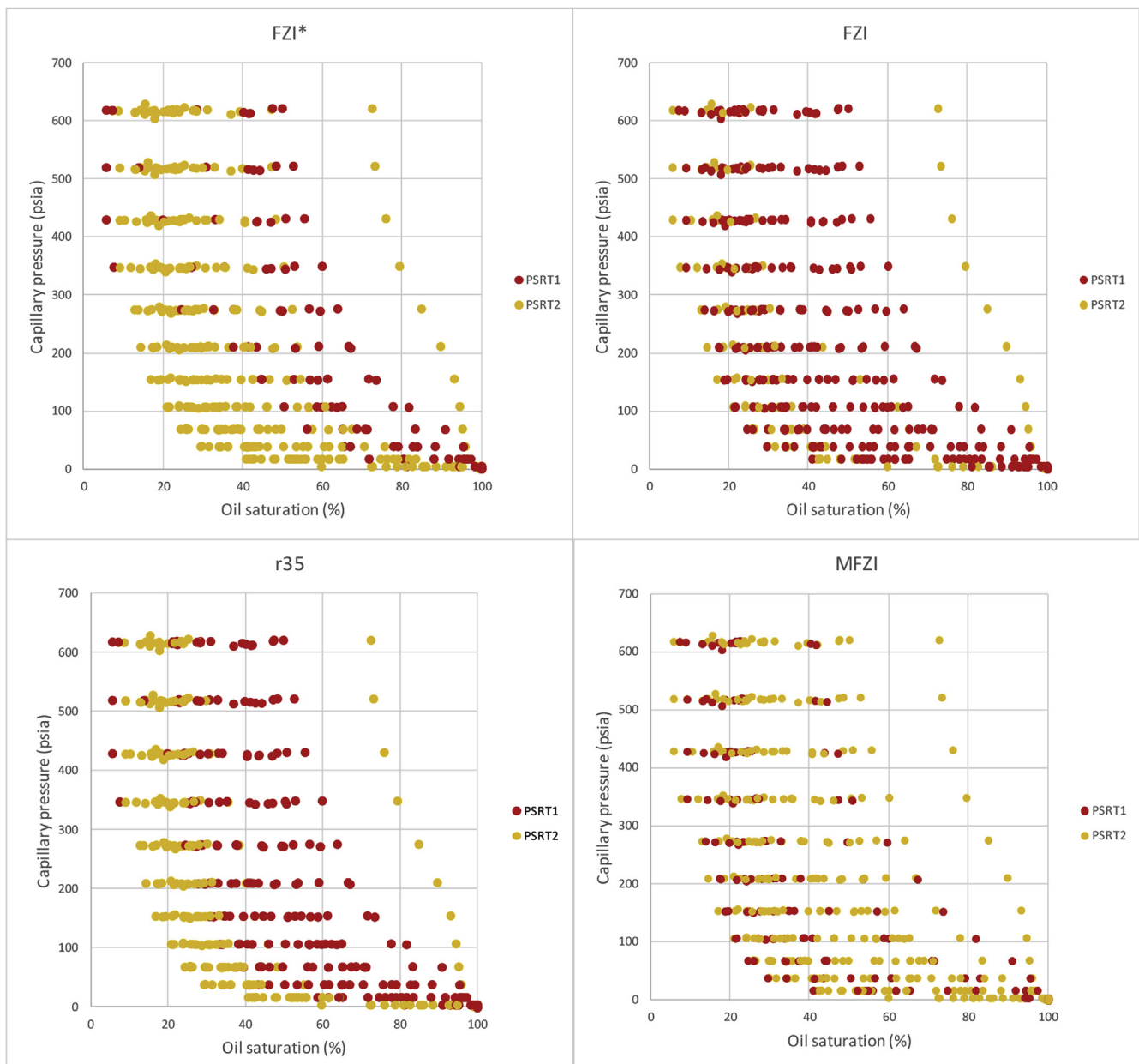


Fig. 6. PSRTs using the gas-oil capillary pressure data (zero connate water saturation) by FZI* (top left), FZI (top right), MFZI (bottom right), and Winland r35 (bottom left).

associated with higher residual oil saturation values. Considering this, all indices, except for the MFZI, decreased as residual oil saturation increased. FZI* and Winland r35 showed a correlation coefficient of 0.2 (each), whereas the R^2 of FZI was found 0.12. MFZI provided the highest R^2 of 0.33 which is mostly due to the fact that MFZI takes into consideration the connate water saturation term in its formula. It should be noted here that the term residual oil saturation was used instead of connate water saturation to calculate MFZI in our primary drainage gas-oil capillary pressure experiments with zero connate water saturation.

The exponential model exhibited the best fit (see Table 1) to our data and the plot of each index vs. C_5 is shown in Supplementary Material. This relationship signifies the FZI* with R^2 of 0.64 followed by Winland r35 with R^2 of 0.55 where both decrease as C_5 increases. The correlation between FZI and C_5 was quite poor (R^2 of 0.01). MFZI with R^2 of 0.2 exhibited an increasing trend unlike FZI* and Winland r35.

Supplementary Material represents the plots of four different indices

vs. C_6 , as well, where all indices except MFZI showed an increase with respect to C_6 with R^2 values of 0.44, 0.45, 0.19, and 0.07 for FZI*, Winland r35, FZI, and MFZI, respectively.

To develop a mathematical expression for FZI* and PSRTI, porous medium was assumed as a simple bundle of capillary tubes (Mirzaei-Paibaman et al., 2018). Such an assumption may not fully represent or capture the complexities associated with porous medium. Nevertheless, even with such simplified models if properly defined, they can resolve challenging petrophysical problems in highly heterogeneous porous media such as carbonates. Considering the application of FZI* in categorizing various existing PSRTs in a medium, the observed anomalies could have originated from lack of $F_{3\tau}$ data in particular. As it was explained earlier, a correct index (i.e., PSRTI) that should be used to study PSRTs ideally is $FZI^* \sqrt{F_{3\tau}}$ instead of FZI*. If one can obtain an accurate estimation of $F_{3\tau}$ and include it in the analysis, such ambiguities and inconsistencies can be resolved, notably.

Another major reason for the underperformance of FZI* in the

appraisal of PSRTs could be due to issues with sample preparation. We assumed that the samples were properly cleaned from drilling fluids and other contaminations prior to experiments to make sure they exhibited the same wetting conditions. However, in practice the cleaning process may still leave behind some contaminations in the samples causing slightly different wettability.

Additionally, if connected porosity is utilized for calculations instead of the effective connected porosity, some overlaps in identified PSRTs, and also PDRTs, can be observed. To be more specific, connected porosity is the one that is measured routinely in laboratory studies and accounts for all connected pore/pore throat sizes, even those small ones that are not contributing to the flow; whereas, effective connected porosity only represents connected pore throats that significantly control the fluid flow through a medium. Hence, if one can measure effective connected porosity and substitute that for connected porosity, better results in petrophysical rock typing will be achieved (Rabiller, 2017; Mirzaei-Paiaman et al., 2018).

4.2. Characterization of PDRTs

4.2.1. Water-oil relative permeability data

PDRTs were investigated by water and oil relative permeability data based on different indices in Figs. 7 and 8. These figures illustrate the strong superiority of FZI* compared to the other methods examined. Despite the fact that PDRTs categorized with this method are well separated, there still exists some areas of overlapping rock types. The reason behind this could be attributed to the use of connected porosity instead of effective connected porosity. Furthermore, aging procedures can generate systems with different wetting conditions. This being said, we should emphasize that FZI* was developed with the assumption of the same wettability among the samples (Mirzaei-Paiaman et al., 2018). Winland r35 also presented a good classification of the PDRTs; while, FZI and MFZI did not produce acceptable results.

The correlation between four different indices and $\frac{k_{ew}}{\phi}$ at S_{or} is displayed in Supplementary Material. All indices showed an increasing

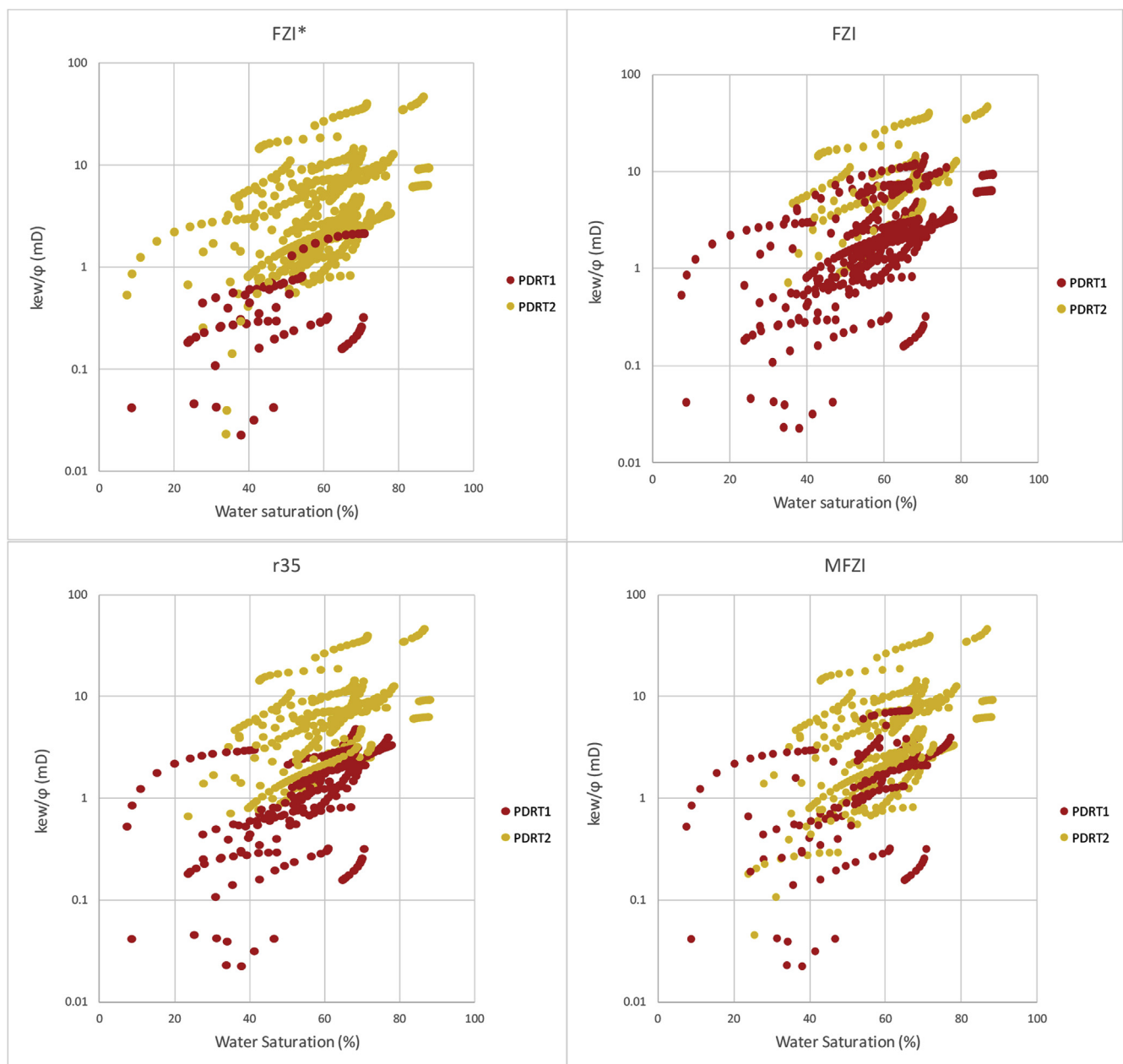


Fig. 7. Identification of PDRTs using water $\frac{k_e}{\phi}$ data by FZI* (top left), FZI (top right), MFZI (bottom right), and Winland r35 (bottom left).

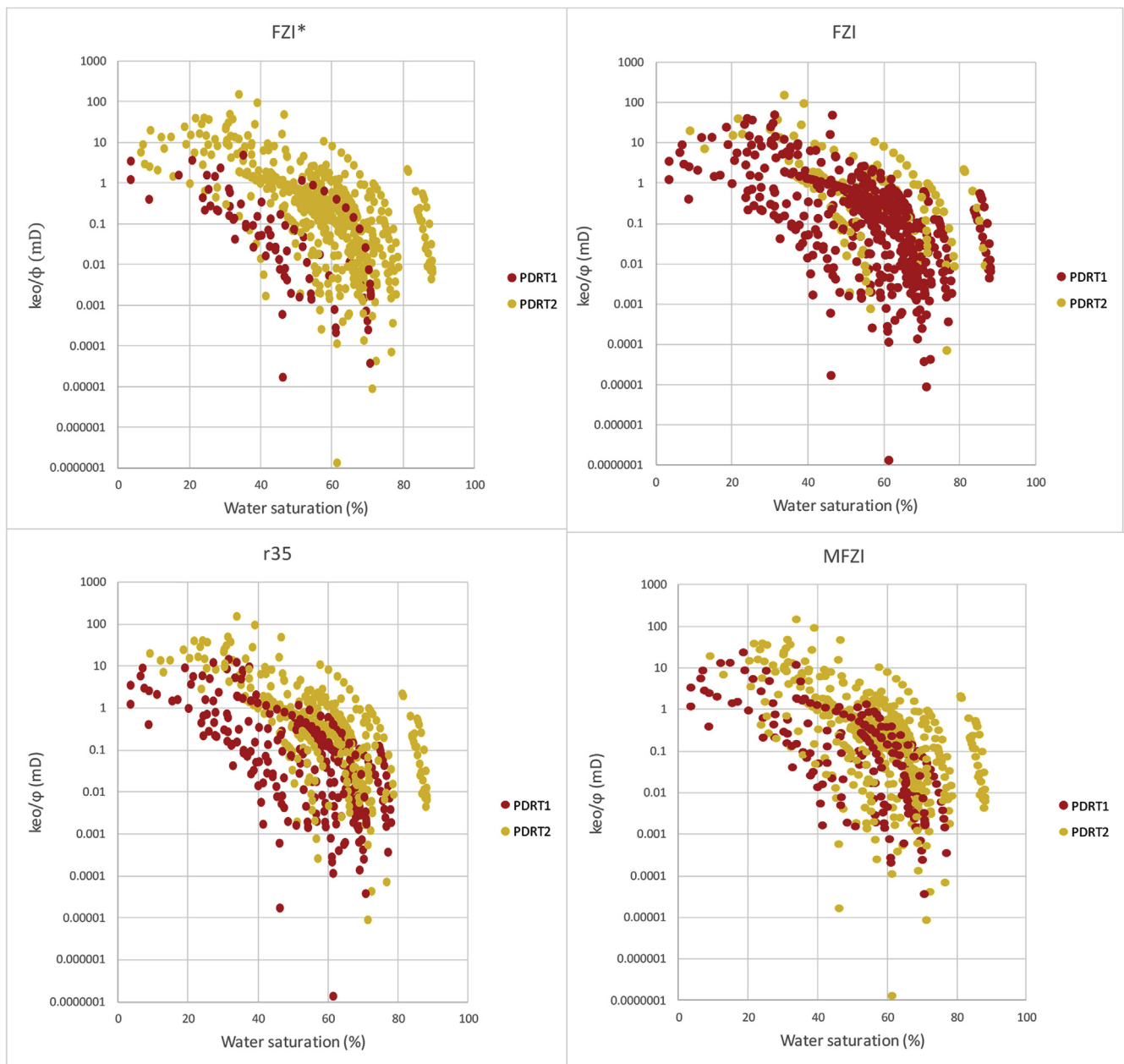


Fig. 8. Identification of PDRTs using oil $\frac{k_e}{\phi}$ data by FZI* (top left), FZI (top right), MFZI (bottom right), and Winland r35 (bottom left).

trend as $\frac{k_{ew}}{\phi}$ increased. FZI* and Winland r35 are found with the highest R^2 values of 0.83 and 0.84, respectively while R^2 of FZI and MFZI were 0.35 and 0.38, respectively. All indices also increased when $\frac{k_{eo}}{\phi}$ at S_{wi} increased. In this regard, FZI* had the highest R^2 of 0.91 followed by 0.87, 0.25, and 0.23 for Winland r35, MFZI, and FZI; respectively. While plotting the indices vs. $\frac{k_e}{\phi}$ at the cross-over point, the point at which $k_{ew} = k_{eo}$, FZI* and Winland r35 generated almost identical R^2 values of 0.81 and 0.82 whereas R^2 values for FZI and MFZI were 0.34 and 0.38; much lower than the other two.

Based on Table 1, exponential and logarithmic equations were found to better fit water and oil $\frac{k_e}{\phi}$ data, respectively. Regarding the water $\frac{k_e}{\phi}$ data in Supplementary Material, the relationship between different indices and C_7 shows that all indices increase as this attribute increases. MFZI, FZI, Winland r35, and FZI* each produced R^2 values of 0.59, 0.55, 0.49, and 0.41, respectively. We did not observe any meaningful relationship between the indices and C_8 . Furthermore, regarding each index vs. C_9 , an increasing trend for FZI* and Winland r35

with the correlation coefficients 0.73 and 0.72 was found, respectively.

4.2.2. Gas-oil relative permeability data

We continued the analysis of PDRTs through gas/oil effective permeabilities for each index displayed in Figs. 9 and 10. From the comparison of these figures it can be concluded that FZI* performed much better in separating PDRTs compared to other indices.

Effective permeability data is controlled strongly by pore structure. In this study, the end-point $\frac{k_{eg}}{\phi}$ (i.e., at residual liquid saturation), end-point $\frac{k_{eo}}{\phi}$, and $\frac{k_e}{\phi}$ at the cross-over point are considered as representative effective permeability data to investigate their relationships with the indices. See Supplementary Material for the correlation between indices and the end-point $\frac{k_{eg}}{\phi}$ data. It was found that all indices increase as the end-point $\frac{k_{eg}}{\phi}$ increases where FZI* and Winland r35 are associated with the highest R^2 values of 0.71 and 0.74, respectively, and FZI and MFZI with the lowest R^2 values of 0.31 and 0.04, correspondingly. Moreover,

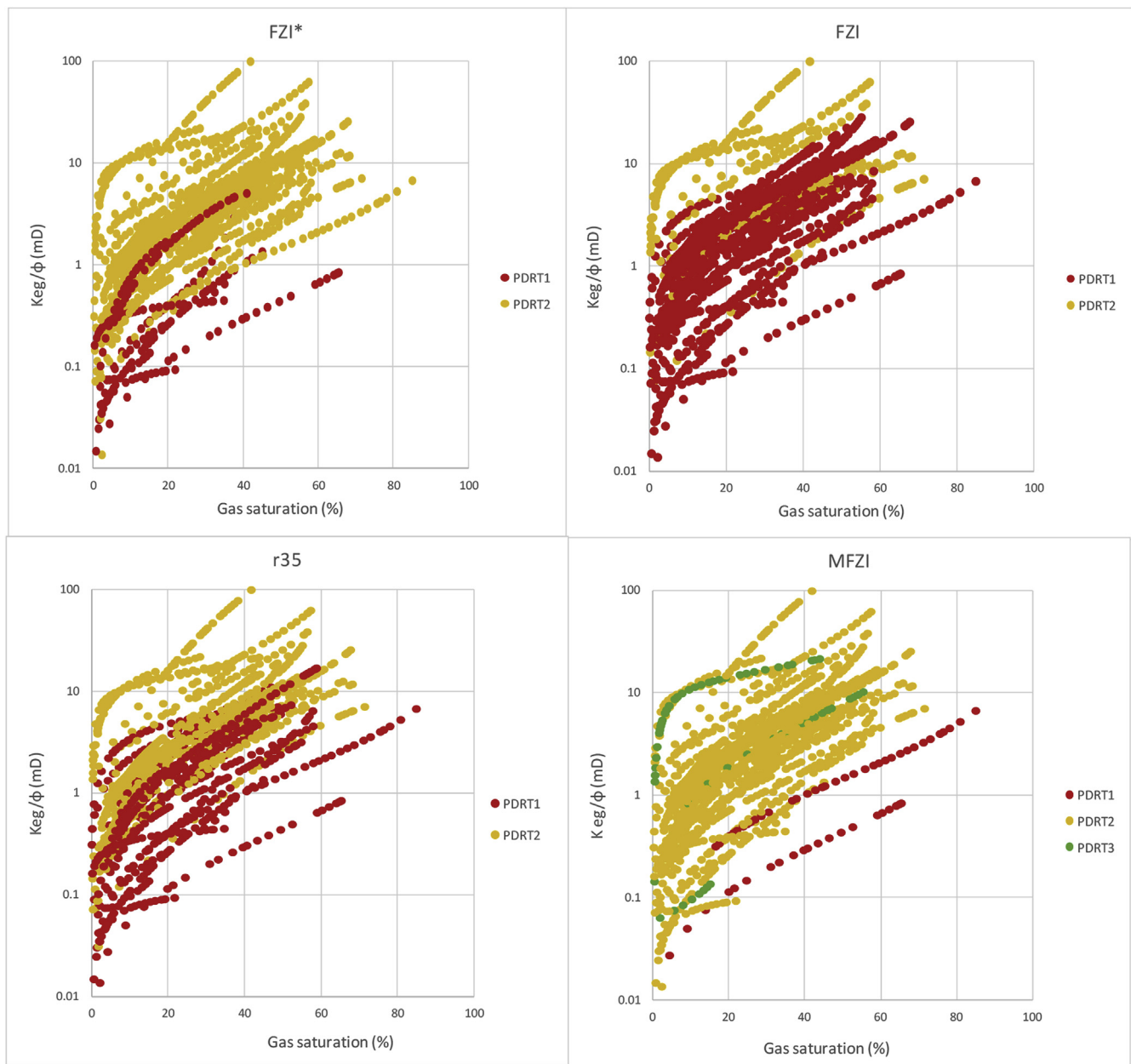


Fig. 9. PDRTs using gas $\frac{k_e}{\phi}$ data by FZI* (top left), FZI (top right), MFZI (bottom right), and Winland r35 (bottom left).

all indices increase as the end-point $\frac{k_{eo}}{\phi}$ increases, where FZI* has the highest R^2 of 0.94 followed by R^2 values of 0.89, 0.24, and 0.03 for Winland r35, FZI, and MFZI, respectively (see Supplementary Material). When plotting the indices vs. $\frac{k_e}{\phi}$ at the cross-over point, as shown in Supplementary Material, FZI* and Winland r35 generated significantly better results than the FZI and MFZI.

Exponential models were better fitted to gas and oil $\frac{k_e}{\phi}$ data (Table 1). Relationships between different indices and C_{10} and C_{11} are shown in Supplementary Material. It was found that as C_{10} increases all indices increase with FZI* showing the highest correlation coefficient. In regards to C_{11} , FZI*, and Winland r35 showed an increasing trend whereas FZI and MFZI showed a decreasing trend. Supplementary Material depicts the relationships between different indices with C_{12} and C_{13} , respectively. As C_{12} increases all indices increase as well, with Winland r35 followed by FZI* and FZI presenting the best performances. Similar to C_{11} , as C_{13} increased, FZI* and Winland r35 both increased as well, while FZI and MFZI decreased.

The details of correlation coefficients found in plotting different indices vs. constants/attributes are summarized in Table 2. In 13 out of 25 cases FZI* produced the highest R^2 s while in 8 cases Winland r35 gave the highest correlation coefficients. In addition in 4 cases these two indices almost matched. This reveals that theoretically-based FZI* and empirical Winland r35 result in the highest R^2 s with the FZI* outperforming the Winland r35. Mirzaei-Paibaman et al. (2018) showed that almost all empirical indices, including Winland r35, have a similar mathematical format and can be considered as the special solution of our proposed FZI*/PSRTI model. Among these special solutions Winland r35 showed an acceptable performance in our case. It should be emphasized here that Winland r35, since is empirical, may not have such a good performance in other reservoirs and this requires further investigation.

5. Conclusions

In this paper, we attempted to compare the accuracy of previous

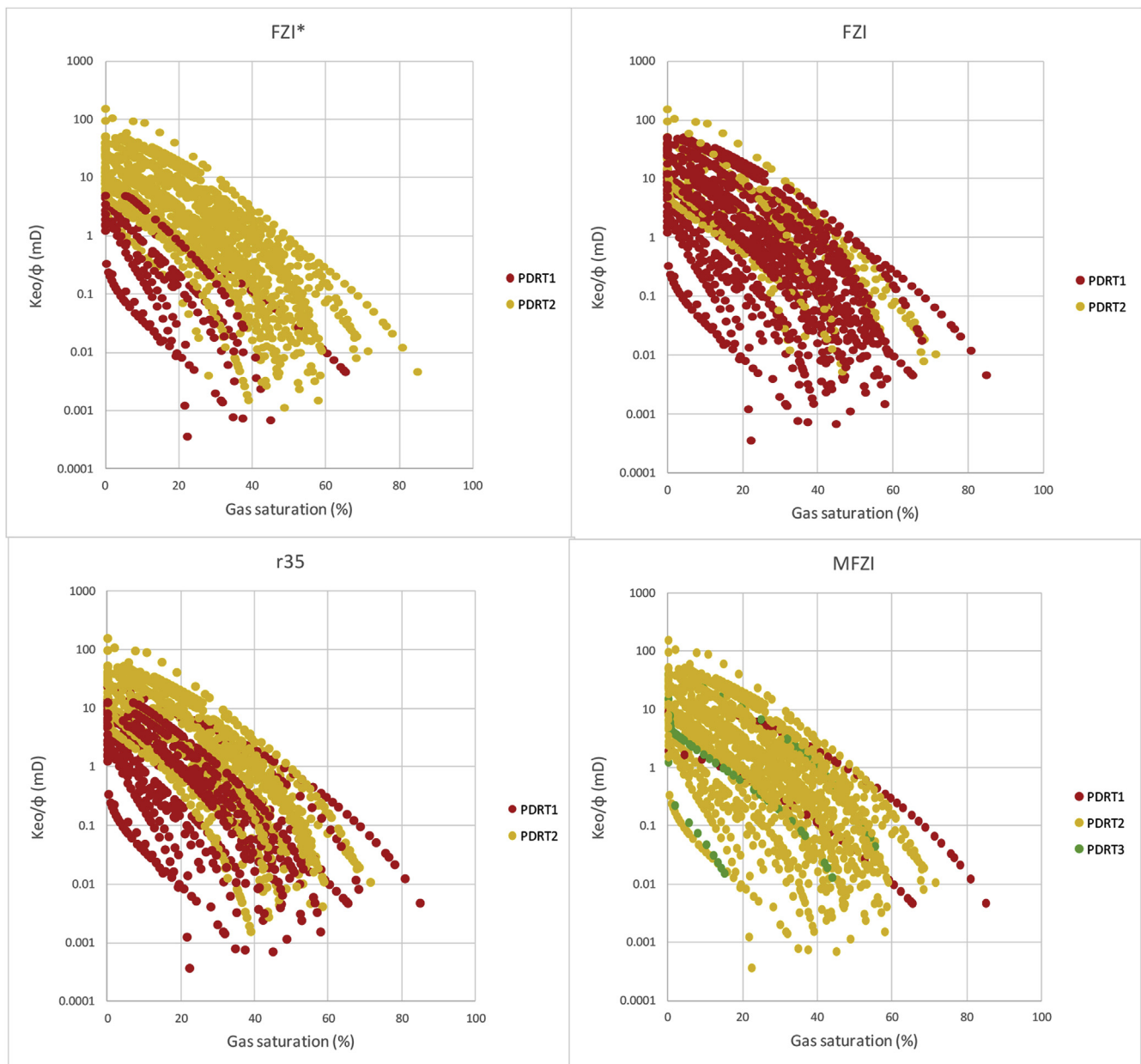


Fig. 10. PDRTs using oil $\frac{k_e}{\phi}$ data by FZI* (top left), FZI (top right), MFZI (bottom right), and Winland r35 (bottom left).

(FZI, Winland r35, and MFZI) and recent (FZI* and PSRTI) petrophysical rock typing indices in appraisal of static and dynamic rock groups by utilizing a significant amount of SCAL data from a heterogeneous carbonate formation. Based on our analyses the following 6 conclusions can be drawn:

1. In many practical circumstances, static and dynamic rock types are not the same and exhibit significant differences. Although the previous methods fail in recognizing such differences, the FZI* and PSRTI are able to distinguish between static and dynamic rock types.
2. The indices FZI* and PSRTI can identify various groups of static and dynamic rock types better than the existing ones. The occasional underperformance of these two indices could mainly be attributed to lack of some essential petrophysical data such as effective connected porosity, tortuosity, and shape factor. Cleaning and aging procedures could be other factors affecting the rock typing outcome.
3. Regarding the correlation between various indices and several petrophysical attributes, FZI* and PSRTI give the most acceptable

results.

4. The PSRTs and PDRTs identified by PSRTI and FZI*, respectively, can be used with high confidence in water saturation-height calculations and fluid displacement simulation processes.
5. Saturation functions (e.g., water-oil capillary pressure) cannot always be modeled using a specific form of a mathematical function (e.g. exponential model).
6. Among the special solutions of the FZI* (e.g., FZI, MFZI, and Winland r35) the empirical Winland r35 showed an acceptable performance in rock typing study. This index may not have such a good performance in other reservoirs and needs further investigations.

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Table 2

Correlation coefficients between different indices and petrophysical parameters.

Test	Parameter	FZI*	FZI	MFZI	Winland r35
Primary drainage mercury injection capillary pressure data	Threshold pressure	0.66	0.01	–	0.61
	Measured r35	0.84	0.05	–	0.84
	Area under the capillary pressure curve	0.67	0.16	–	0.59
	C ₁	0.75	0.05	–	0.76
Primary drainage water-oil capillary pressure data	C ₂	0.71	0.10	–	0.73
	Connate water saturation	0.58	0.03	0.57	0.48
	C ₃	0.53	0.04	0.20	0.47
Primary drainage gas-oil capillary pressure data (non-zero connate water saturation)	Residual liquid saturation	0.97	0.93	0.73	0.97
	C ₄	0.52	0.29	0.11	0.51
Primary drainage gas-oil capillary pressure data (zero connate water saturation)	Residual oil saturation	0.20	0.12	0.33	0.20
	C ₅	0.64	0.01	0.20	0.55
	C ₆	0.44	0.19	0.07	0.45
	End-point $\frac{k_{ew}}{\phi}$	0.83	0.35	0.38	0.84
Water-oil relative permeability data	End-point $\frac{k_{eo}}{\phi}$	0.91	0.23	0.25	0.87
	Cross-over point $\frac{k_e}{\phi}$	0.81	0.34	0.38	0.82
	C ₇	0.41	0.55	0.59	0.49
	C ₈	0.00	0.06	0.14	0.00
	C ₉	0.73	0.20	0.25	0.72
	End-point $\frac{k_{eg}}{\phi}$	0.71	0.31	0.04	0.74
	End-point $\frac{k_{eo}}{\phi}$	0.94	0.24	0.03	0.89
	Cross-over point $\frac{k_e}{\phi}$	0.76	0.33	0.05	0.74
	C ₁₀	0.53	0.09	0.02	0.49
	C ₁₁	0.12	0.01	0.16	0.09
Gas-oil relative permeability data	C ₁₂	0.67	0.34	0.05	0.73
	C ₁₃	0.08	0.02	0.21	0.06

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Appendix A. Supplementary data

Supplementary data to this article can be found online at <https://doi.org/10.1016/j.petrol.2019.01.014>.

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