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Parametric Modelling and Multi-Objective Optimization of Electro Discharge Machining Process Parameters for Sustainable Production

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Abstract: Electro Discharge Machining (EDM) can be an element of a sustainable manufacturing system. In the present study, the sustainability implications of EDM of special-purpose steels are investigated. The machining quality (minimum surface roughness), productivity (material removal rate) improvement and cost (electrode wear rate) minimization are considered. The influence and correlation of the three most important machining parameters including pulse on time, current and pulse off time have been investigated on sustainable production. Empirical models have been established based on response surface methodology for material removal rate, electrode wear rate and surface roughness. The investigation, validation and deeper insights of developed models have been performed using ANOVA, validation experiments and microstructure analysis respectively. Pulse on time and current both appeared as the prominent process parameters having a significant influence on all three measured performance metrics. Multi-objective optimization has been performed in order to achieve sustainability by establishing a compromise between minimum quality, minimum cost and maximum productivity. Sustainability contour plots have been developed to select suitable desirability. The sustainability results indicated that a high level of 75.5% sustainable desirability can be achieved for AISI L3 tool steel. The developed models can be practiced on the shop floor practically to attain a certain desirability appropriate for particular machine limits.

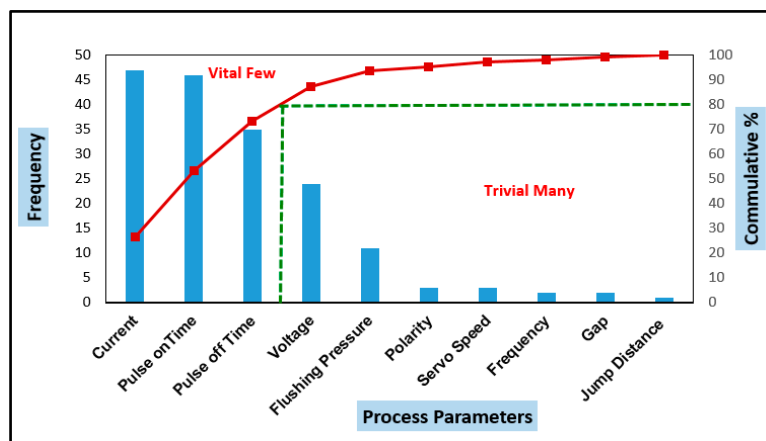
Keywords: electric discharge machining; response surface methodology; sustainability; productivity; cost; surface quality; microstructure

1. Introduction

The enormously growing demand for tool steel during the last decades is due to its embedded properties including wear resistance, corrosion resistance, hardness and exceptional property of retaining cutting end at exalted temperatures. Moreover, its cost-effectiveness also makes it an ideal candidate over carbides, titanium and inconel materials. Therefore, tool steel is being extensively employed for tools and die manufacturing in automotive, nuclear and aerospace industries [1,2]. Tool steel is commercially available in a number of series such as D, A, H, L and M. L series is a special purpose low alloy steel and is available in a number of grades including L1, L2, L3, L6 and

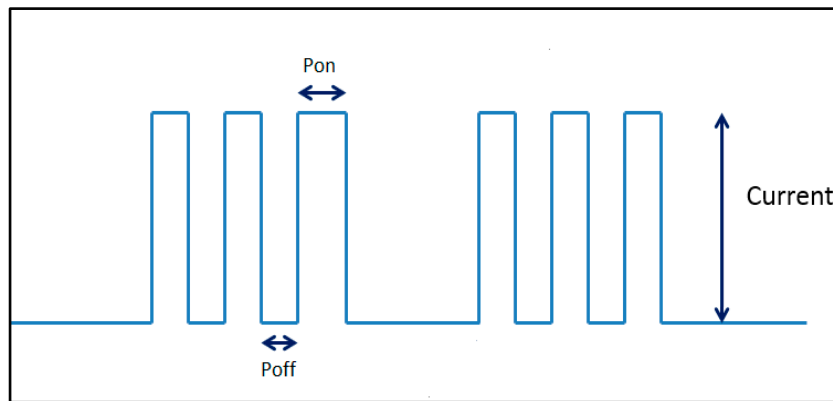
L7 [3]. Due to hard to cut nature of tool steels, their machining through conventional methods results in dimensional inaccuracies, residual stresses and higher surface roughness and tool wear. These limitations in conventional techniques of machining are being addressed by utilizing non-conventional or special purpose machining processes. Electric discharge machining (EDM) is a non-conventional machining process used for manufacturing complex profiles with accuracy [4]. Minimum chattering, residual stresses and mechanical vibration are eminent advantages obtained by EDM owing to the absence of direct interaction of tool with work part while machining.

With a growing competition of production rates among industries, there is a visible increase in resources utilization and emissions of toxic materials to the environment. This has initiated a sustainability study of manufacturing systems and technologies. Sustainability has three pillars—the environmental, economic and the social. Sustainability in manufacturing is concerned with the manufacturing of products having minimum adverse environmental effect, safety of employees, conservation of natural resources and energy and are economically viable for customers. Machining is a major constituent of manufacturing system and sustainability in machining is related to environmental friendliness (cutting fluids), minimum cost and energy consumption, higher production and quality, better waste management and safety of worker [5]. The productivity, cost and quality of electric discharge machined parts are measured through performance measures: material removal rate (MRR), electrode wear rate (EWR) and surface roughness (SR) respectively [6]. Machining performance measures are directly associated with process parameters including pulse on time (Pon), current, pulse off time (Poff), voltage, flushing pressure, polarity, servo speed, frequency, gap and jump distance as shown in Figure 1a. The illustration of selected process parameters (Pon, Poff and current) is presented in Figure 1b. The Pareto chart is based on a detailed literature review of more than fifty research papers published in the last 15 years for electric discharge machining of tool steel (only those papers are selected in which MRR, EWR and SR separately or in combination have been evaluated). For investigating the influence of process parameters on productivity, cost and quality of electric discharged machined part, it can be observed from Figure 1 that current, pulse on time (Pon) and pulse off time (Poff) are widely applicable process parameters as identified by researchers.



(a)

Figure 1. Cont.



(b)

Figure 1. (a) Pareto chart for process parameters selection (b) Selected process parameters.

Literature also suggests that the current and Pon has a direct influence on MRR, EWR and SR; all three performance measures increase when current is increased [7–26]. Whereas, Pulse off time exhibits inverse effects that are, MRR, EWR and SR decrease at higher Poff [19,25]. Moreover, It had also been reported that Poff does not significantly influence MRR, EWR and SR [22].

Different mathematical and statistical approaches have been presented by various researchers for modelling and optimization of performance measures related to EDM of tool steel. These techniques include conventional methods, taguchi (orthogonal array), response surface methodology (RSM), genetic algorithm (GA), fuzzy logic and grey relational analysis (GRA) [7–10,16–18,23–26]. The application of these techniques for different tool steel materials is presented in Figure 2 [7–43]. The figure represents a literature summary of experimental works for different tool steels along with performance measures and experimental techniques. Each performance measure is indicated by a symbol as shown in Figure 2.

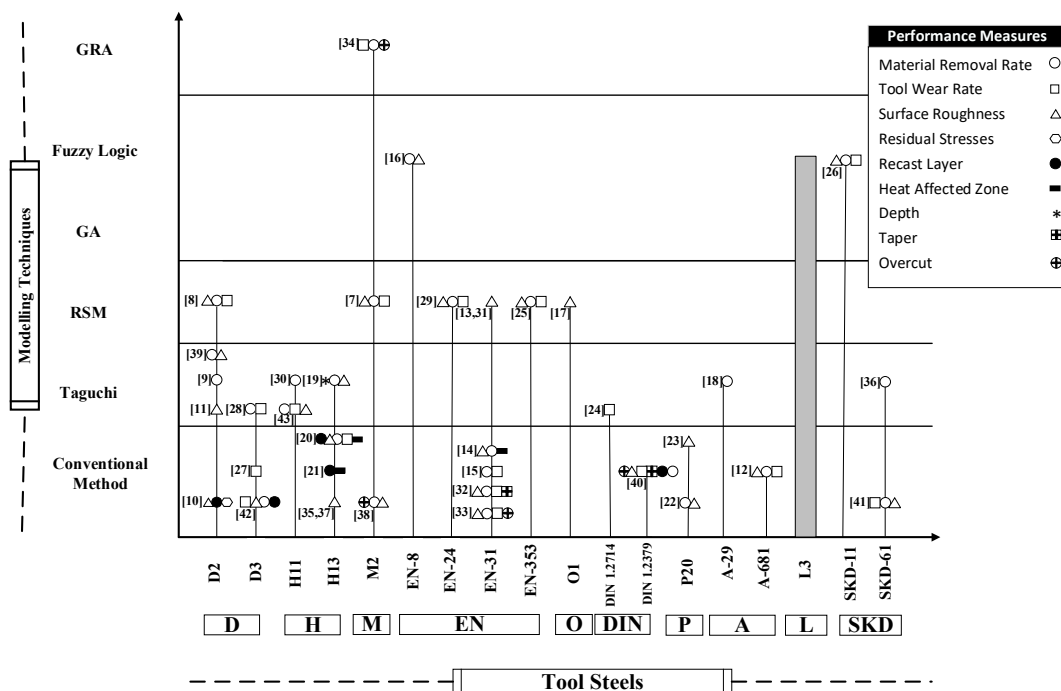


Figure 2. Literature review.

Although various researchers have attempted to investigate and model the impact of process parameters on EWR, SR and MRR, limited or no research has been reported on special-purpose low alloy tool steel (AISI L3) to predict MRR, EWR and SR. Furthermore, literature reveals that productivity and quality are inversely related [22,25] and current and pulse on time are the most decisive factors [44]. Productivity increases with high-energy consumption (higher values of current and pulse on time), whereas quality improves at low energy utilization (lower current and pulse on time) as observed by Mandaloi et al. [7], Payal et al. [14] and Singh et al. [15] for machining AISI M2 and EN-31 tool steels.

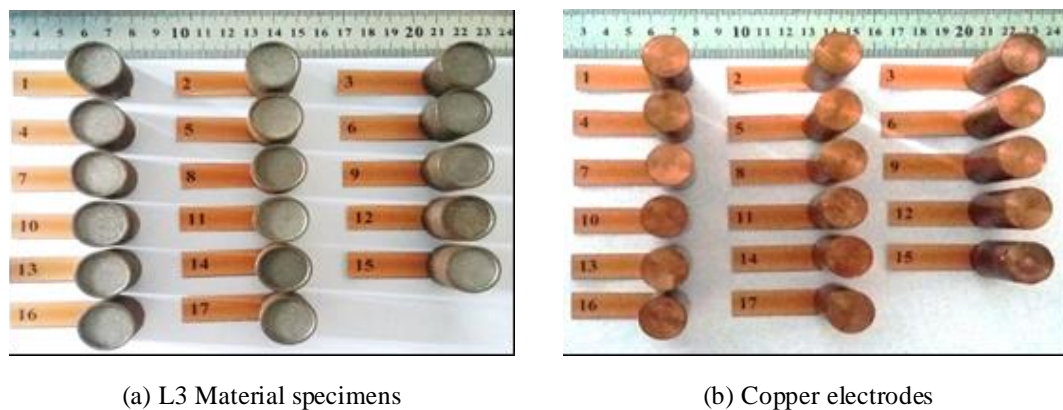
Sustainability in machining operation is related to different aspects such as tool life, surface quality of machined parts, production ratio, energy consumption, environment issues, usage of lubricants and coolants and safety and welfare of workers. All these elements are broadly classified as economic, environmental and social pillars of sustainability considering a machining operation [45]. This research aims to achieve sustainable production based on the economic aspect of sustainability while electric discharge machining of low alloying special-purpose AISI L3 tool steel. L3 alloy is selected as it possesses higher hardenability, because of higher percentages of Cr, V and C which make it suitable for making tools and dies. Empirical models have been derived adopting Response Surface Methodology (RSM) for MRR, EWR and SR and adequacy of models have been checked by analysis of the variance (ANOVA). Analysis of process parameters has been performed using surface plots. Moreover, sustainability has been achieved employing desirability based multi-objective optimization. In the end, micrographs have been discussed to reveal the machined surface in terms of voids, pits and micro-cracks.

2. Experimental Procedure

This segment illustrates the chemical properties of the material, preparation of material samples and tools, experimental setup and measurement of responses. Experiments have been performed on AISI L3 tool steel, the chemical composition is presented in Table 1. All samples of work material were prepared by extracting cylindrical samples having 20 mm length and 22 mm diameter, while copper rods in the form of cylindrical shape having dimensions 50.8 mm \times 19 mm (length \times diameter) were employed as electrodes as shown in Figure 3a,b respectively. The machining was performed on die-sinker electric discharge machine CM655C (75 N). Workpieces and electrodes were subjected to grinding and polishing before conducting experiments.

Table 1. Chemical properties of AISI L3 low alloy tool steel.

Composition	C	Cr	Mn	P	Si	S	V	Fe
Weightage (%)	1.02	1.3	0.59	0.01	0.32	0.01	0.18	Balance



(a) L3 Material specimens

(b) Copper electrodes

Figure 3. Samples of work material.

Three process parameters including, (i) current, (ii) pulse on time (Pon) and (iii) pulse off time (Poff) were investigated for machining AISI L3 tool steel. During each experiment, the material was removed up-to a depth of 1.5 mm and to ensure the uniformity of machining a new electrode was used for each experimental run. Moreover, each experimental run was repeated thrice (three times) to accurately estimate the variation in the obtained values and to avoid uncertainty in the results.

The productivity, cost and quality of electric discharge machined parts were measured using MRR, EWR and SR respectively. Moreover, the analysis of the microstructure of the samples was performed for surface quality evaluation. Before taking micrographs, samples were treated firstly by dipping them into a well-prepared mixture of resin and hardener and then dried for stabilization. Micrographs have been taken using the Scanning Electron Microscope (SEM), TESCAN (MIRA 3 XMU type). All micrographs were taken in nanospace, keeping 101× magnification and 10 kV High Voltage (HV) value. Weight difference method was used for the measurement of MRR and EWR [46–48]. For this purpose, weight balance Mettler PE 1600 was used before and after the individual experiment. The following relations (Equations (1) and (2)) were used for the calculation of MRR and EWR.

$$\text{MRR (mm}^3/\text{min)} = \frac{W_p \text{ (g)} - W_a \text{ (g)}}{\text{Machining Time (min)} \times \text{Density (g/mm}^3\text{)}} \quad (1)$$

$$\text{EWR (mm}^3/\text{min)} = \frac{E_p \text{ (g)} - E_a \text{ (g)}}{\text{Machining Time (min)} \times \text{Density (g/mm}^3\text{)}} \quad (2)$$

where W_p and W_a are the weights of workpieces prior to machining and afterwards; whereas, E_p and E_a are the weights of electrodes prior to machining and afterwards. Compressed air followed by dipping in acetone was employed to remove debris and kerosene remains on machined specimens. Surface roughness (SR) was recorded by surface roughness meter, SJ-410-Surftest. Three observations were made at random locations and the average was taken as final reading for further analysis.

3. Experimental Design

The higher and lower levels for the three parameters are chosen based on the literature review and trial runs as long as the machined parts remained within the acceptable quality range. The selected parameters together with their chosen ranges are provided in Table 2. Modelling and analysis of performance measures (MRR, EWR and SR) have been carried out through RSM employing the Box Behnken Design (BBD). Overall, seventeen (17) experimental runs were performed with twelve (12) factorial and five (5) center points. The experimental runs along with process parameters and observed values of performance measures have been presented in Table 3.

Table 2. Process parameters with their levels.

Process Parameters	Levels		
	Low	Middle	High
Pulse On Time (μs)	200	400	600
Current (A)	10	13	16
Pulse Off Time (μs)	50	100	150

Table 3. Design matrix.

Exp Run	Process Parameters			Performance Measures		
	Pulse On Time	Current	Pulse Off Time	Material Removal Rate	Electrode Wear Rate	Surface Roughness
	(Pon)		(Poff)	(MRR)	(EWR)	(SR)
	μs	A	μs	mm^3/min	mm^3/min	μm
1	200	10	100	1.57	1.14	0.64
2	600	10	100	3.49	2.59	1.18
3	200	16	100	2.84	1.77	3.10
4	600	16	100	8.46	4.58	3.58
5	200	13	50	3.07	1.39	1.65
6	600	13	50	5.30	2.50	2.40
7	200	13	150	0.77	1.00	1.20
8	600	13	150	5.49	4.09	1.63
9	400	10	50	4.77	2.24	1.21
10	400	16	50	8.70	3.56	3.56
11	400	10	150	4.57	2.64	0.67
12	400	16	150	6.42	3.57	3.10
13	400	13	100	7.50	3.11	2.10
14	400	13	100	7.80	3.00	2.19
15	400	13	100	7.69	3.26	2.23
16	400	13	100	7.72	3.12	2.12
17	400	13	100	7.77	3.11	2.22

4. Results, Analysis and Discussions

This section is comprised of results discussion and statistical analysis using RSM. Moreover, mathematical model selection and adequacy confirmation through ANOVA are discussed. Influences of process parameters on performance measures have been evaluated using 3D graphs (surface plots).

4.1. Development of Empirical Models

Modelling of the performance measures MRR, EWR and SR have been performed through regression analysis using commercial software (Design Expert ®10.06). Analysis of Variance have been used to test the significance of factors and developed models.

4.1.1. Material Removal Rate (MRR)

After detailed experimentation, linear, quadratic and cubic models were tested to select the fitted model. The results revealed quadratic expression as the preferable model for material removal rate (MRR) (based on minimum p-value and R^2 , adjusted R^2 and predicted R^2 (close to 1)). The results obtained through ANOVA are presented in Table 4. It can be observed that main effects Pon (A), current (B), poff (C), interaction effects Pon and current (AB), Pon and Poff (AC), current and Poff (BC) and quadratic effects Pon (A^2), current (B^2) and Poff (C^2) were the significant terms of MRR model. The statistical measures R^2 , adjusted R^2 and predicted R^2 have also been provided. From the results, it is evident that the fitted regression model is significant at 95% confidence interval with 'p' value under 0.05. Furthermore, resulted values of statistical terms (R^2 , adjusted R^2 and predicted R^2) are nearly 1 which depicted that model is satisfactory to adopt. The resulted empirical model for MRR is provided in Equation (3).

$$\begin{aligned}
 \text{MRR} = & -22.22697 + (0.043425 \times \text{Pon}) + (1.88978 \times \text{Current}) + (0.089232 \times \text{Poff}) \\
 & + (1.54167 \times 10^{-3} \times \text{Pon} \times \text{Current}) + (6.225 \times 10^{-5} \times \text{Pon} \times \text{Poff}) \\
 & - (3.46667 \times 10^{-3} \times \text{Current} \times \text{Poff}) - (7.57938 \times 10^{-5} \times \text{Pon}^2) \\
 & - (0.063806 \times \text{Current}^2) - (4.027 \times 10^{-4} \times \text{Poff}^2)
 \end{aligned} \tag{3}$$

Table 4. ANOVA results for material removal rate, electrode wear rate and surface roughness.

Material Removal Rate					
Source	Sum of Squares	df	Mean Square	F Value	p-Value Prob > F
Model	100.14	9	11.13	546.97	<0.0001
A-Pon	26.25	1	26.25	1290.18	<0.0001
B-Current	18.06	1	18.06	887.81	<0.0001
C-Poff	2.63	1	2.63	129.46	<0.0001
AB	3.42	1	3.42	168.25	<0.0001
AC	1.55	1	1.55	76.20	<0.0001
BC	1.08	1	1.08	53.17	0.0002
A ²	38.70	1	38.70	1902.51	<0.0001
B ²	1.39	1	1.39	68.26	<0.0001
C ²	4.27	1	4.27	209.79	<0.0001
Residual	04	7	0.020		
Lack of Fit	0.087	3	0.029	2.10	0.2432
Pure Error	0.055	4	0.014		
Cor. Total	100.28	16			
Std. Dev.	0.14			R-Squared	0.9986
Mean	5.53			Adj. R-Squared	0.9968
C.V. %	2.58			Pred. R-Squared	0.9852
PRESS	1.48			Adeq Precision	73.693

Electrode wear rate					
Source	Sum of Squares	df	Mean Square	F Value	p-value Prob > F
Model	15.82	7	2.26	104.91	<0.0001
A-Pon	8.95	1	8.95	415.23	<0.0001
B-Current	2.96	1	2.96	137.60	<0.0001
C-Poff	0.32	1	0.32	15.04	0.0037
AB	0.46	1	0.46	21.46	0.0012
AC	0.98	1	0.98	45.49	<0.0001
A ²	1.92	1	1.92	89.18	<0.0001
C ²	0.16	1	0.16	7.23	0.0248
Residual	0.19	9	0.022		
Lack of Fit	0.16	5	0.032	3.74	0.1129
Pure Error	0.034	4	8.55×10^{-3}		
Cor. Total	16.02	16			
Std. Dev.	0.15			R-Squared	0.9879
Mean	2.75			Adj. R-Squared	0.9785
C.V. %	5.35			Pred. R-Squared	0.9398
PRESS	0.96			Adeq Precision	35.252

Surface roughness					
Source	Sum of Squares	df	Mean Square	F Value	p-value Prob > F
Model	13.42	7	1.92	653.02	<0.0001
A-Pon	0.61	1	0.61	206.02	<0.0001
B-Current	11.62	1	11.62	3955.57	<0.0001
C-Poff	0.62	1	0.62	209.78	<0.0001
AC	0.026	1	0.026	8.72	0.0162
A ²	0.22	1	0.22	76.51	<0.0001
B ²	0.14	1	0.14	48.54	<0.0001
C ²	0.21	1	0.21	70.03	<0.0001
Residual	0.026	9	2.937×10^{-3}		
Lack of Fit	0.013	5	2.51×10^{-3}	0.72	0.6406
Pure Error	0.014	4	3.47×10^{-3}		
Cor. Total	13.45	16			
Std. Dev.	0.054			R-Squared	0.9980
Mean	2.05			Adj. R-Squared	0.9965
C.V. %	2.65			Pred. R-Squared	0.9905
PRESS	0.13			Adeq Precision	79.960

4.1.2. Electrode Wear Rate (EWR)

The fit model details for electrode wear rate (EWR) also confirms that the quadratic expression is the most suitable relationship (based on minimum p-value and R^2 , adjusted R^2 and predicted R^2 (close to 1)). The regression terms (main effect, interaction and quadratic) which are significant for EWR include Pon (A), current (B) and Poff (C), Pon and current (AB) and Pon and off (AC), Pon (A^2) and Poff (C^2), respectively. The ANOVA results along with adequacy measures have been provided in Table 4. The resulted empirical model with less than 0.5 'p' value is shown in Equation (4) that can be used successfully for prediction.

$$\begin{aligned} \text{EWR} = & -0.54243 + (6.46294 \times 10^{-3} \times \text{Pon}) - (0.023750 \times \text{Current}) \\ & - (4.06579 \times 10^{-4} \times \text{Poff}) + (5.66667 \times 10^{-4} \times \text{Pon} \times \text{Current}) \\ & + (4.95 \times 10^{-5} \times \text{Pon} \times \text{Poff}) - (1.68651 \times 10^{-5} \times \text{Pon}^2) \\ & - (7.68421 \times 10^{-5} \times \text{Poff}^2) \end{aligned} \quad (4)$$

4.1.3. Surface Roughness (SR)

The details of the fit model for surface roughness also recommended the quadratic model as the most appropriate model (based on minimum p-value and R^2 , adjusted R^2 and predicted R^2 (close to 1)). Pon (A) current (B) and Poff (C) main terms, Pon and Poff (AC) interaction terms and Pon (A^2), current (B^2) and Poff (C^2) quadratic terms have significant effects on surface roughness model. The ANOVA results including regression terms have been demonstrated as Table 4. The developed model is valid because it illustrated a good relationship between parameters and performance measure as 'p' value is under 0.05 (Confidence interval= 95). Moreover, the obtained values of regression metrics are approximately 1 which establish the suitability of model. The empirical model of surface roughness is presented in Equation (5) which is effective for prediction.

$$\begin{aligned} \text{SR} = & -1.71756 + (6.795 \times 10^{-3} \times \text{Pon}) - (0.12989 \times \text{Current}) + (0.015330 \times \text{Poff}) \\ & - (8 \times 10^{-6} \times \text{Pon} \times \text{Poff}) - (5.775 \times 10^{-6} \times \text{Pon}^2) + (0.020444 \times \text{Current}^2) \\ & - (8.84 \times 10^{-5} \times \text{Poff}^2) \end{aligned} \quad (5)$$

4.2. Validation of Model

Statistical analysis has been conducted to assure the fitness of regression models. Furthermore, for experimental validation of empirical models, additional confirmation experiments have been performed. In order to confirm either the developed model are the best representation of actual responses, normal probability plots have been plotted as shown in Figures 4a–6a for MRR, EWR and SR respectively. It is observed that the residuals generally fall on a straight line implying that the errors are normally distributed. Moreover, the comparison plots of predicted against actual values of performance measures MRR, EWR and SR are established and shown in Figures 4b–6b respectively. These plots confirm the normal distribution of error for all responses since all the theoretically assumed (predicted) and actual response values lie on the recommended straight-line or in its close approximation. Consequently, the established models are appropriate and are less likely to violate assumptions.

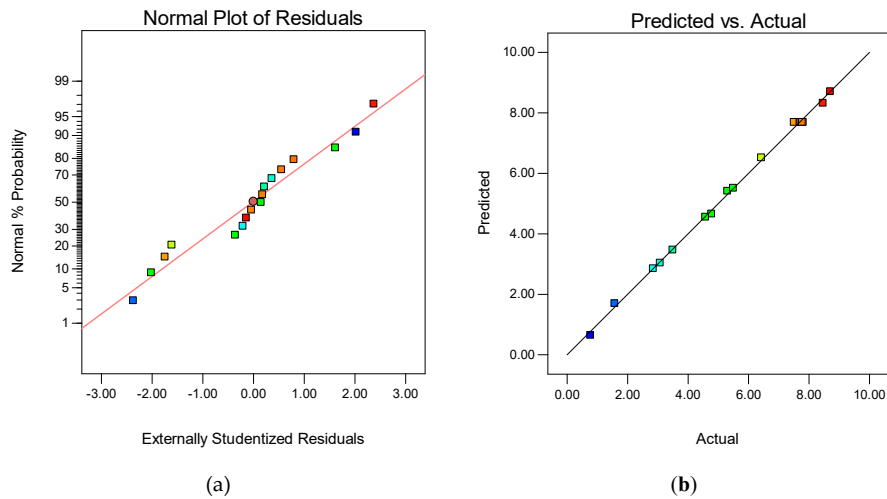


Figure 4. (a) Normal probability plot of residuals and (b) Predicted versus actual responses for material removal rate (MRR).

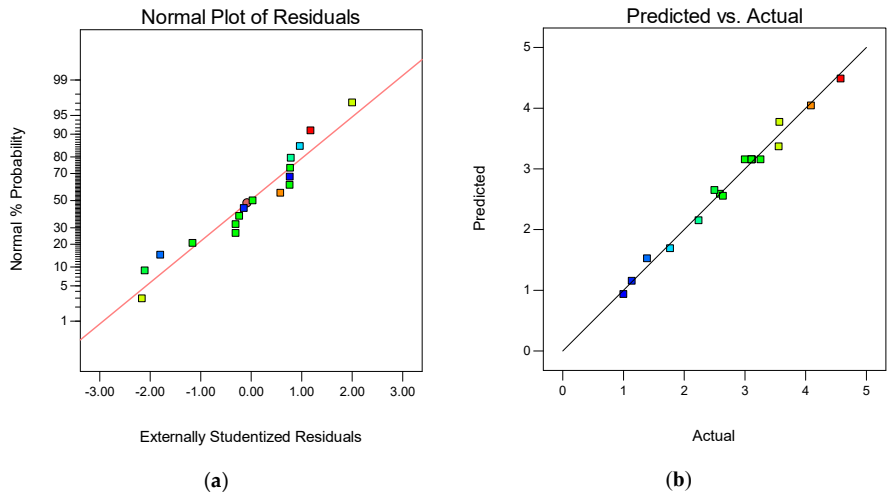


Figure 5. (a) Normal probability plot of residuals and (b) Predicted versus actual responses electrode wear rate (EWR).

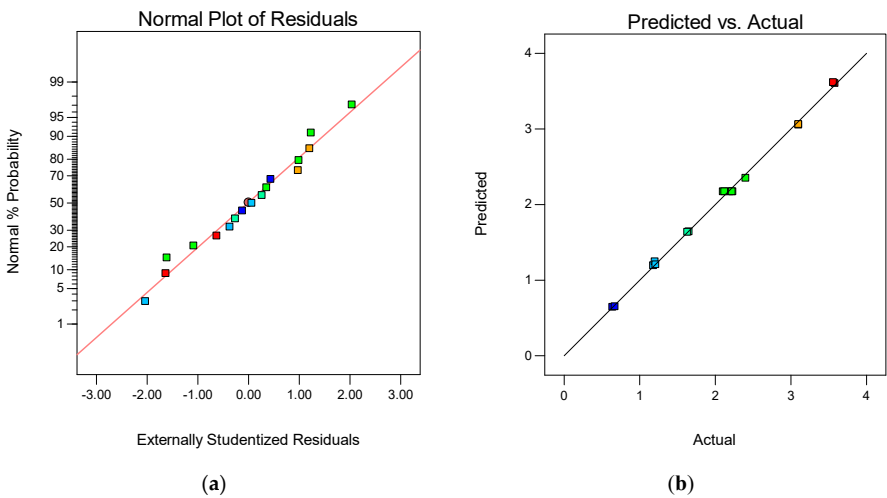


Figure 6. (a) Normal probability plot of residuals and (b) Predicted versus actual responses for surface roughness (SR).

To validate the established empirical models, six (6) verification experimental runs were designed by randomly selecting the values of process parameters within design space (the selected levels were different from the designed values used for model development). The results of validation experiments and corresponding percentage error have been provided in Table 5. The percentage error value was calculated by using Equation (6) [48–50].

$$\text{Percentage Error} = \left| \frac{\text{Actual value} - \text{Predicted value}}{\text{Predicted value}} \right| \times 100 \quad (6)$$

Table 5. Evaluation of predicted and actual performance measures.

Run No.	Process Parameters			Performance Measures						Percentage Error		
	Pon	Current	Poff	Predicted			Actual			MRR	EWR	SR
				MRR	EWR	SR	MRR	EWR	SR			
μs	A	μs	mm^3/min	mm^3/min	μm	mm^3/min	mm^3/min	μm	%	%	%	
1	300	12	80	5.75	2.30	1.66	5.96	2.24	1.61	3.65	2.6	3.01
2	500	12	80	7.00	3.04	1.96	7.18	2.93	1.92	2.57	3.61	2.04
3	300	12	120	5.18	2.26	1.8	5.38	2.24	1.88	3.80	0.89	4.4
4	500	14	120	8.10	3.92	2.51	8.18	3.87	2.57	0.98	1.28	2.39
5	300	14	120	5.73	2.55	2.27	5.56	2.63	2.31	2.9	3.14	1.76
6	500	14	80	8.45	3.56	2.77	8.57	3.64	2.8	1.42	2.25	1.08

The established mathematical models are found valid as the percentage error is under 5%. Hence, these established models are effectively applicable for the prediction of performance measures in future.

4.3. 3D Response Surface

The effects of process parameters on material removal rate (MRR), electrode wear rate (EWR) and surface roughness (SR) have been presented in 3D response surface plots (Figures 7–9).

4.3.1. Material Removal Rate (MRR)

The influence of both Pon and current on material removal rate (MRR) have been presented as a surface plot in Figure 7a. In the beginning, MRR increases as Pon increases up to a maximum value of 8.80 mm^3/min and after that decreases. Contemporarily, a positive relationship exists between MRR and current, that is, MRR increases as current increases since maximum discharge energy enhances the material removal phenomena. Furthermore, Pon is the most influencing process parameter than current. Figure 7b describes the influence of Pon and Poff on MRR. Higher MRR is observed at the lower value of Poff and middle value of Pon. The correlation of MRR with Poff and current has been shown as 3D graph in Figure 7c. The graph confirms gradual increment in MRR along with increasing values of current. Conversely, Poff has an inverse effect on MRR. MRR increases as current and Pon increases because maximum discharge energy become available and deeper, and overlying craters are produced as a result of concentrated heat and localized melting. The trends are similar to those observed by Mandaloi et al. [7], Payal et al. [14], Sultan et al. [25] and Lin et al. [26].

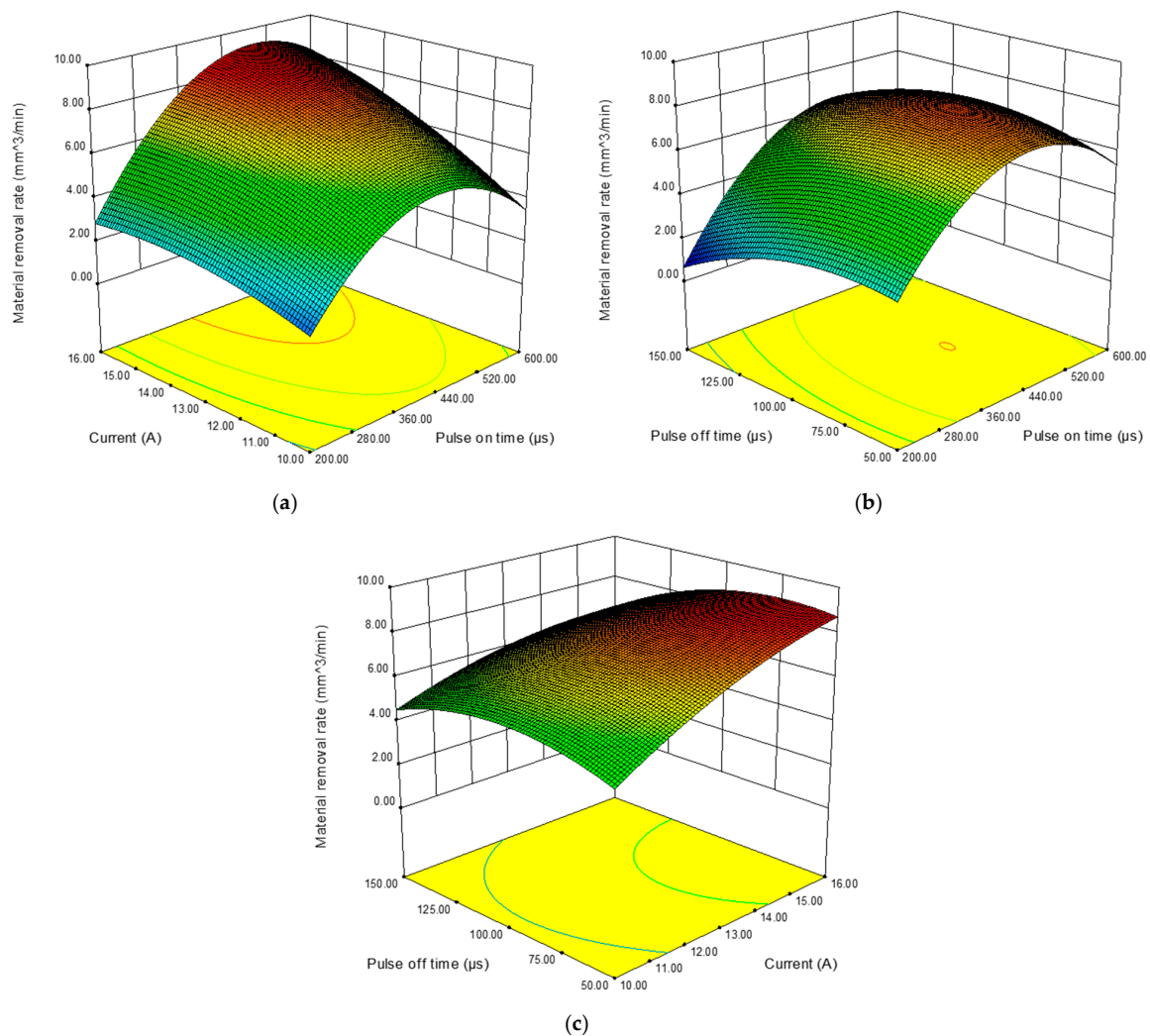


Figure 7. Response surface graphs showing the effects of (a) Pon and current, (b) Pon and Poff and (c) current and Poff on material removal rate.

4.3.2. Electrode Wear Rate (EWR)

Figure 8a presents the influence on electrode wear rate (EWR) when changing Pon and current. It is evident from the figure that Pon has more influence than current. Furthermore, EWR increases by increasing Pon and current. The highest value of EWR is observed at maximum values of Pon and current. The response of Poff and Pon on EWR have been presented in Figure 8b. The Figure clearly indicates that EWR is minimum at the lower value of Pon and high value of Poff and maximum at high level of Pon and low level of Poff. Moreover, EWR is relatively more affected by Pon than Poff. The surface plot of Poff and current (shown in Figure 8c) indicates that EWR is in direct relation with the current while Poff has an inverse effect on EWR. Maximum EWR resulted at higher values of current and Pon because more powerful discharging occurs with higher energy density that melts and removes more material from electrode. Similar effects have been observed by Sultan et al. [25] and Lin et al. [26].

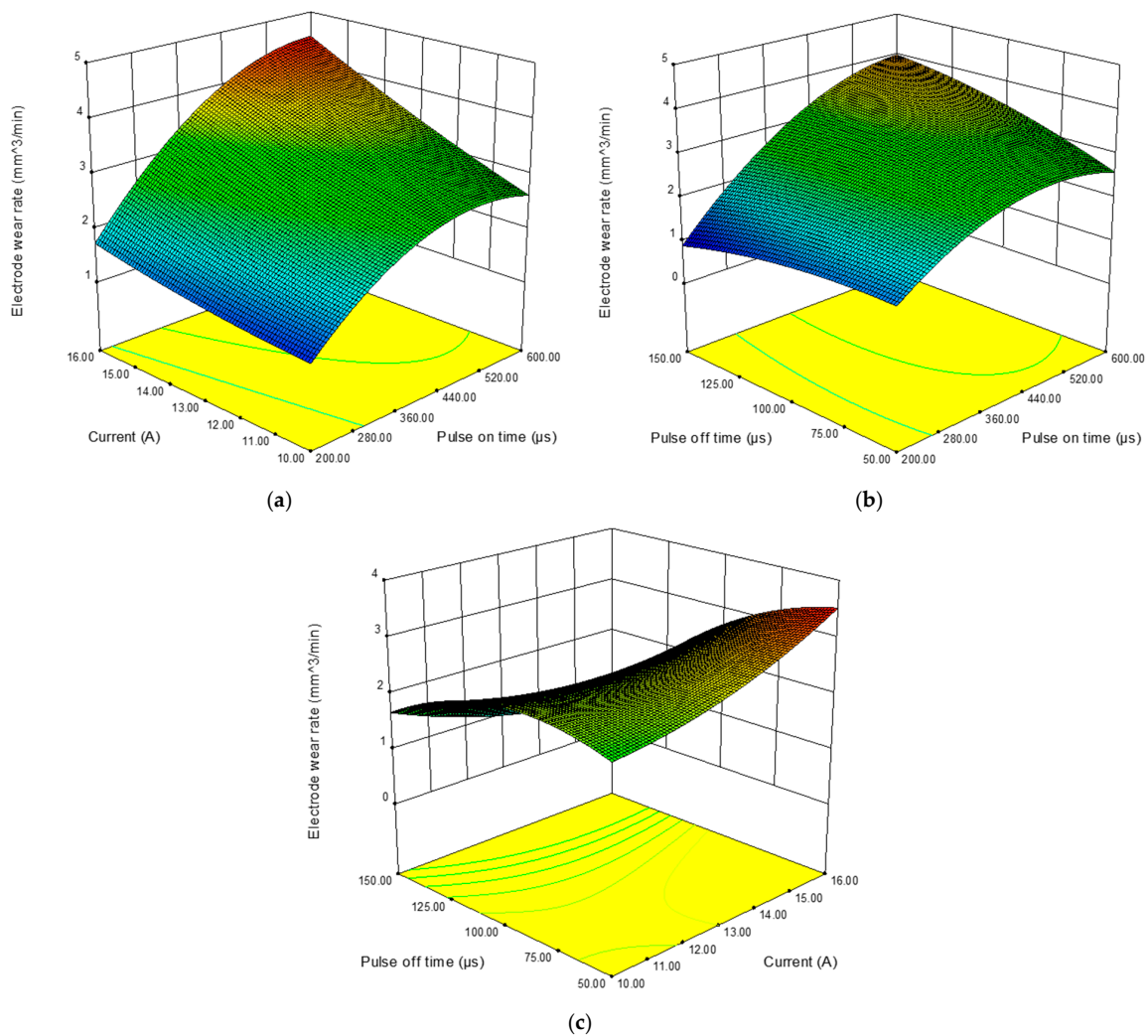


Figure 8. Response surface graphs showing the effects of (a) Pon and current, (b) Pon and Poff and (c) current and Poff on electrode wear rate.

4.3.3. Surface Roughness (SR)

The plot of surface roughness (SR) based on Pon and current indicates that SR increases as both current and Pon increase (Figure 9a). Furthermore, SR is significantly influenced by current than Pon. The 3D plot of Pon and Poff with SR is presented in Figure 9b. It is evident from the figure that minimum SR can be achieved at lower value of Pon and Poff. The effects of current and Poff is displayed in Figure 9c. The figure depicts that SR increases with the increase in current. Whereas, Poff has a negligible influence on SR. At higher levels of current, discharge energy becomes greater which enhances the erosion and melting of material and hence, surface roughness increases as stated by Sultan et al. [25] and Lin et al. [26].

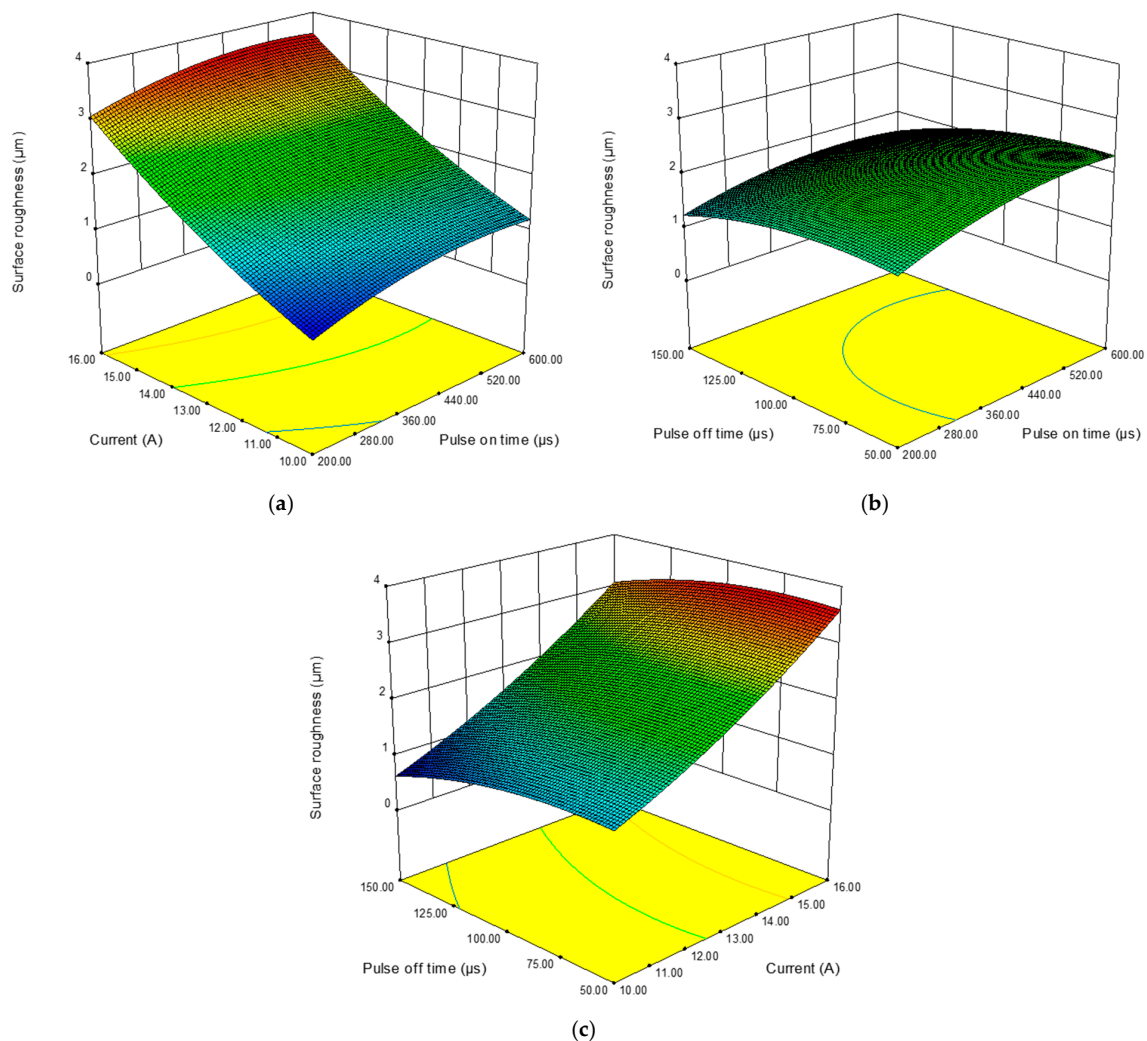


Figure 9. Response surface graphs showing the effects of (a) Pon and current, (b) Pon and Poff and (c) current and Poff on surface roughness.

5. Optimization Associated with Sustainability

Sustainable machining aims to achieve high production rate at minimum cost while maintaining the highest quality standards. Simultaneous optimization of these objective functions leads to minimum environmental damage and thereby assures sustainable production. The performance measures for the current research include MRR, EWR and SR. The sustainability function is the combination of three objective functions and is given by the relation 7.

$$\text{Sustainability} = \begin{cases} \text{Maximize MRR (Productivity)} \\ \text{Minimize EWR (Cost)} \\ \text{Minimize SR (Quality)} \end{cases} \quad (7)$$

On the basis of detailed analysis of empirical models and 3D response surfaces presented in previous sections, relationships of process parameters with respect to performance measures have been presented in Table 6. The table represents a comparison of two functions, “as-is” function versus “to-be” function. Here, “as-is” function characterizes achieved effects on performance measures (MRR, EWR and SR) while increasing level of the three process parameters (Pon, Current and Poff), for example, MRR, EWR and SR increase by increasing Pon and Current and vice versa. On the other hand, “to-be” function depicts the norm for desired sustainability. For instance, the objective function is to maximize

MRR, while minimizing EWR and SR, whereas, in reality, all performance measures (MRR, EWR and SR) increase with the increase in Pon. Similar results are achieved by increasing current. Increase in Poff, on the other hand, leads to sustainable EWR and SR with compromised MRR.

Table 6. As-is and To-be sustainability function.

Parameters	As-Is Function (Achieved Function)			To-Be Sustainability Function (Desired Sustainability Function)		
	MRR	EWR	SR	MRR	EWR	SR
A: Pon	↑	↑	↑	↑	↓	↓
B: Current	↑	↑	↑	↑	↓	↓
C: Poff	↓	↓	↓	↓	↑	↑

Notation: ↑ represents increasing function and ↓ represents decreasing function.

From the above discussion, it can be concluded that the simultaneous optimization of these performance measures cannot be attained directly. To overcome this problem, multi-objective optimization has been carried out considering desirability. The purpose of the desirability function is to combine the effects of multiple responses into a single desirability value using mathematical transformation. This multi-objective optimization-based desirability has been accomplished in two stages namely (i) desirability identification and (ii) formulation of combined desirability geometric mean (CDGM). During the desirability identification stage, each performance measure Y_i is converted into a single desirable value d_i having range $0 \leq d_i \leq 1$, where 0 indicates the most undesirable value and 1 depicts the most desirable value. Once the desirability of individual performance measure has been obtained, they were combined into a single value using geometric mean. The desirability functions for maximizing MRR, minimizing EWR and SR and combined desirability geometric mean (CDGM) have been presented in Equations (8), (9) and (10) respectively [51–53].

$$d_i = \begin{cases} 0, & Y_i \leq L_i \\ \left(\frac{H_i - Y_i}{H_i - L_i}\right)^w, & L_i < y_i < H_i \\ 1, & Y_i \geq H_i \end{cases} \quad (8)$$

$$d_i = \begin{cases} 0, & Y_i \leq L_i \\ \left(\frac{H_i - Y_i}{H_i - L_i}\right)^w, & L_i < y_i < H_i \\ 1, & Y_i \geq H_i \end{cases} \quad (9)$$

$$DGM = (d_1 \times d_1 \times \dots \times d_n^{w_n})^{\frac{1}{n}}, \quad (10)$$

where H_i , L_i , w and n represent higher value, lower value, weight associated with a performance measure and number of performance measures respectively. The multi-objective optimization goals along with the conditions used for desirability approach have been provided in Table 7. All performance measures and process parameters are given equal weights (1) for both upper and lower limits and similarly equal importance value (3) for optimization. The process parameters values and achieved desirability are presented in Table 8. It is evident (from Table 8) that desirability values up to 75.5% have been achieved when all performance measures were given equal weights.

Table 7. Conditions for optimization.

Condition	Units	Goal	Limits		Weights		Importance
			Lower	Upper	Lower	Upper	
A:Pon	μs	In range	200	600	1	1	3
B:Current	μs	In range	10	16	1	1	3
C:Poff	A	In range	50	150	1	1	3
MRR	mm^3/min	Maximize	1.90	6.40	1	1	3
EWR	mm^3/min	Minimize	1.49	4.23	1	1	3
SR	μm	Minimize	1.47	5.11	1	1	3

Table 8. Achieved desirability.

No.	Pon	Current	Poff	MRR	EWR	SR	Desirability	Remarks
	μs	A	μs	mm^3/min	mm^3/min	μm		
1	220.21	13.17	50.00	4.47186	1.80364	2.01094	0.755	Selected
2	220.13	13.21	50.00	4.48082	1.80449	2.02074	0.755	
3	215.90	13.28	50.00	4.45033	1.7644	2.03568	0.755	

The corresponding values of process parameters and performance measures have been presented in Figure 10. The achievable ranges of performance measures are $1.9 \text{ mm}^3/\text{min}$ to $6.4 \text{ mm}^3/\text{min}$ for MRR, $1.5 \text{ mm}^3/\text{min}$ to $4.2 \text{ mm}^3/\text{min}$ for EWR and $1.47 \mu\text{m}$ to $5.10 \mu\text{m}$ for SR as shown in Figure 10. However, with maximum desirability of 75.5%, $4.47 \text{ mm}^3/\text{min}$ of MRR, $1.8 \text{ mm}^3/\text{min}$ of EWR and $2.01 \mu\text{m}$ SR can only be achieved. Practically on the shop floor, where machines exhibit different ranges, the process planners have the constraints of limited selection of process parameters values. For such critical situations, the contour plots (Figure 11a–c) can be employed to use the available values with certain sustainability. For example, at 13A current and $400 \mu\text{s}$ Pon, only 62.9% sustainability can be obtained (Figure 11a).

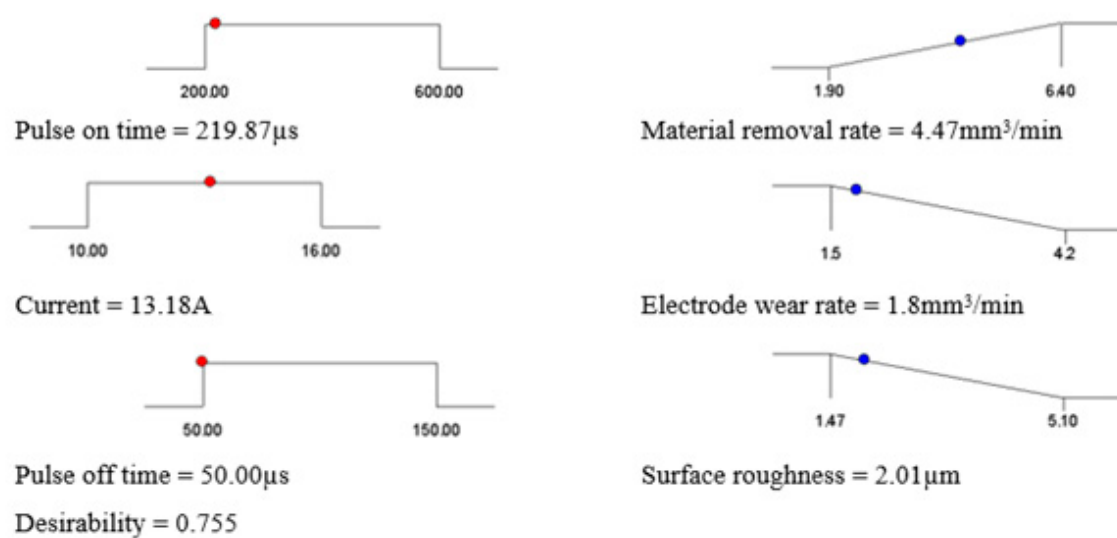


Figure 10. Achievable range of performance measures against specific process parameters range with desirability 0.755.

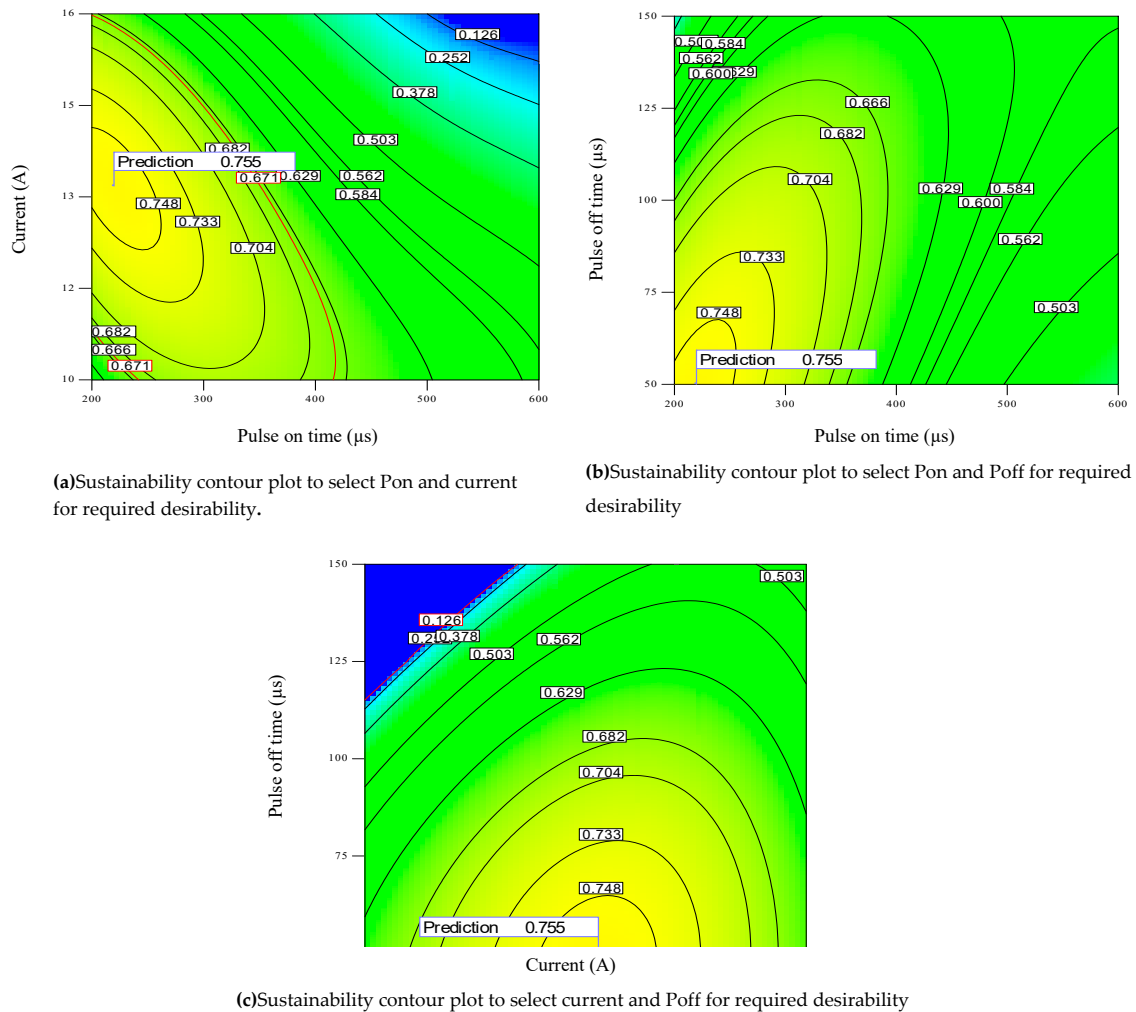


Figure 11. Sustainability contour plot to select parameters for required desirability.

6. Microstructures Analysis

In order to have an explicit understanding of process parameters (Pon, current and Poff) on performance measures (MRR, EWR and SR), microstructures of machined parts have also been examined. Three samples were taken at low, middle and high levels of Pon and current while keeping Poff at the middle value of 100 μs . It is pertinent to mention that in this study, only Pon and current have been identified as the most significant process parameters as compared to Poff. The microstructures graphs of varying current and Pon have therefore been considered for detailed investigation. The microstructures graphs of samples are presented as Figure 12a–c). From Figure 12a, it is manifested that at lower levels of current and Pon (10 A and 200 μs) fewer numbers of craters, debris, globules, pits and voids are visible with minute level micro-cracks. Whereas an increase in the size of micro-cracks, debris, globules, pits craters and voids can be observed at middle levels of current (13 A) and Pon (400 μs), as presented in Figure 12b. Moreover, samples obtained at 16 A current (upper level) and Pon (600 μs) exhibited prominent micro-cracks, craters, debris, globules, pits and voids (Figure 12c). This clearly indicates that increase in current and Pon results in higher cracks, large globule size, pits and voids. This is due to increase vaporization at higher level of current and Pon.

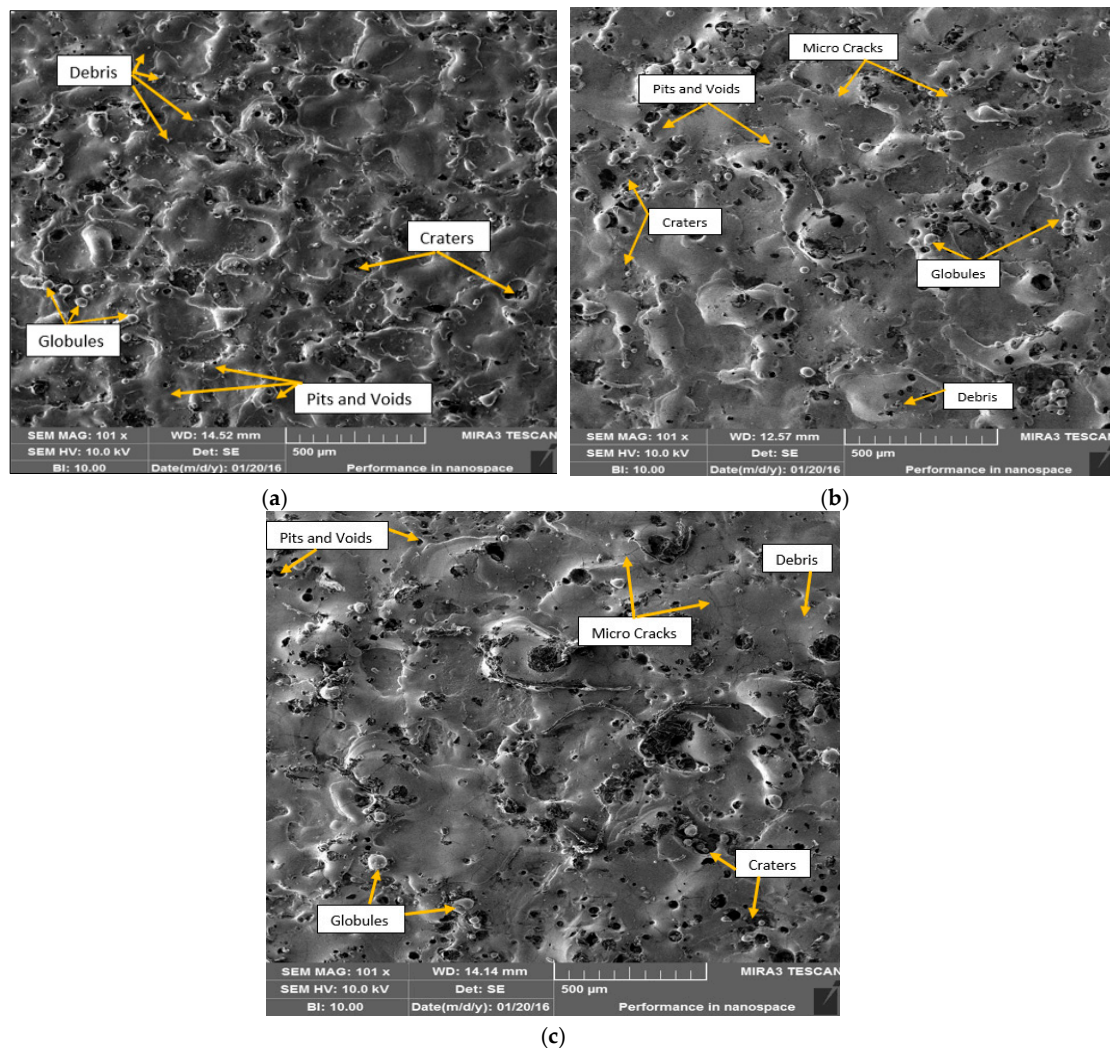


Figure 12. Scanning electron microscope (SEM) microstructures (a) at lower level of current (10 A) and Pon (200 μs), (b) at intermediate level of current (13 A) and Pon (400 μs), (c) at higher level of current (16 A) and Pon (600 μs).

7. Conclusions

The aim of this research was sustainable production by the enhancement of productivity and quality along with cost minimization during EDM of a low alloy tool steel (AISI L3). Initially, empirical models have been developed by analyzing the performance measures (MRR, SR and EWR) through response surface methodology. After that, multi-objective optimization, considering the sustainability, has been executed by instituting a compromise among productivity (MRR maximization), cost (EWR minimization) and quality (SR minimization). From the present investigation, the following interpretations can be concluded:

- Pon and current are the most significant process parameters influencing performance measures, MRR, EWR and SR, to a great extent.
- The higher values of MRR (productivity) can be achieved by keeping both Pon and current at their higher settings with Poff at its lower level. Conversely, lower values of SR and EWR (quality and cost) can be maintained at lower agreeable level of both Pon and current and upper level of Poff.
- By performing multi-objective optimization while incorporating the sustainability measures, maximum MRR of 4.47 mm³/min, minimum EWR of 1.8 mm³/min and SR of 2.01 μm is obtained

as compared to individual values obtained for maximum MRR ($6.4 \text{ mm}^3/\text{min}$), minimum EWR ($1.5 \text{ mm}^3/\text{min}$) and minimum SR ($1.47 \text{ }\mu\text{m}$).

- The microstructure analysis highlighted that the increase in Pon and current results in prominent micro-cracks, craters, debris, globules, pits and voids due to increase in vaporization at the high level of Pon and current.
- The established sustainability contour plots can be employed successfully for feasible machine limits to attain a certain level of desirability.

Further research should evaluate the environmental aspect of sustainability using electric discharge machining. Besides, other performance measures like white/ grey recast layer and cost-based models should be investigated for improvement and enrichment of machining performance.

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