Thermodynamic properties of non-isothermal plasma of ICF

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In this work dense non-ideal, non-isothermal plasma of ICF (inertial confinement fusion) was considered. Correct calculation of plasma properties requires taking into account parameters of plasma. For this purpose interaction potentials of particles were used. The electron-ion temperature in [1] was used in the form $T_{\alpha\beta} = \sqrt{T_{\alpha}T_{\beta}}$.

Effective screened interaction potentials taking into account the quantum-mechanical effect of diffraction were used [2-3]:

$$\Phi_{\alpha\beta}(r) = \frac{Z_{\alpha}Z_{\beta}e^{2}}{r} \frac{1}{\gamma^{2}\sqrt{1 - \left(2k_{D}/\lambda_{ee}\gamma^{2}\right)^{2}}} \times \left(\left(\frac{1/\lambda_{ee}^{2} - B^{2}}{1 - B^{2}\lambda_{\alpha\beta}^{2}}\right)\exp(-Br) - \left(\frac{1/\lambda_{ee}^{2} - A^{2}}{1 - A^{2}\lambda_{\alpha\beta}^{2}}\right)\exp(-Ar)\right) - \frac{Z_{\alpha}Z_{\beta}e^{2}}{r} \frac{(1 - \delta_{\alpha\beta})}{1 + C_{\alpha\beta}}\exp(-r/\lambda_{\alpha\beta}),$$
(1)

where $k_D^2 = k_e^2 + k_i^2$ is the screening parameter taking into account the contribution of electrons and ions, $\gamma^2 = k_i^2 + 1/\lambda_{ee}^2$,

$$\begin{split} A^{2} &= \frac{\gamma^{2}}{2} \Biggl(1 + \sqrt{1 - \left(\frac{2k_{D}}{\lambda_{ee}\gamma^{2}}\right)^{2}} \Biggr), B^{2} &= \frac{\gamma^{2}}{2} \Biggl(1 - \sqrt{1 - \left(\frac{2k_{D}}{\lambda_{ee}\gamma^{2}}\right)^{2}} \Biggr), \\ C_{\alpha\beta} &= \frac{k_{D}^{2} \lambda_{\alpha\beta}^{2} - k_{i}^{2} \lambda_{ee}^{2}}{\lambda_{ee}^{2} / \lambda_{\alpha\beta}^{2} - 1}. \end{split}$$

Pair correlation functions were obtained in the exponential approximation:

$$g_{\alpha\beta}(r) = \exp(-\frac{\Phi_{\alpha\beta}(r)}{k_{\rm B}T}),\tag{2}$$

Composition of plasma was studied using the system of Saha equations:

$$\frac{n_0}{n_e n_i} = \frac{g_0}{g_e g_i} \exp\left(\frac{I - \Delta I}{k_B T}\right),$$
(3)

where g_k is statistical weight, ΔI is the lowering of the ionization potential.

Thermodynamic properties were calculated on the basis of effective potentials (1): internal energy $U = \sum_{\alpha} 3/2N_{\alpha}k_{B}T_{\alpha} + U_{N}$, where the correlation energy of interaction is:

$$U_N = 2\pi V \int_0^\infty \sum_{\alpha,\beta} n_\alpha n_\beta \varphi_{\alpha\beta}(r) g_{\alpha\beta}(r) r^2 dr, \qquad (4)$$

and the equation of state:

$$P = P_{id} - \frac{2\pi}{3} \int_{0}^{\infty} \sum_{\alpha,\beta} n_{\alpha} n_{\beta} \frac{\partial \varphi_{\alpha\beta}(r)}{\partial r} g_{\alpha\beta}(r) r^{3} dr, \quad (5)$$

where $P_{id} = n_e k_B T_e + n_i k_B T_i$ is the pressure of ideal plasma, N is the number of particles in the system.

The obtained thermodynamic properties were used for solving the Hugoniot equation [4].

The Hugoniot equation describes the connection between density and pressure of the gas in front of and behind the shock front. Parameters of gas change very rapidly and in a very narrow field with the passage through the shock wave.

References

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